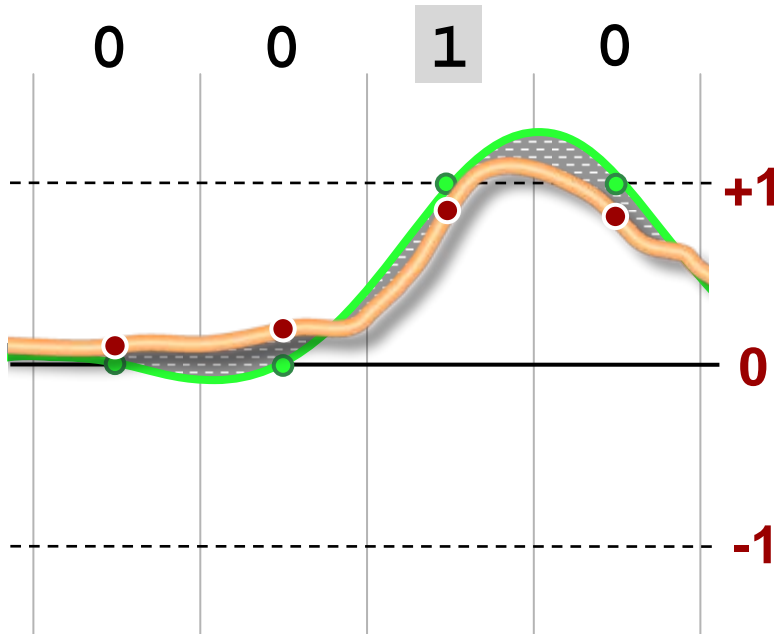


Exhibit A

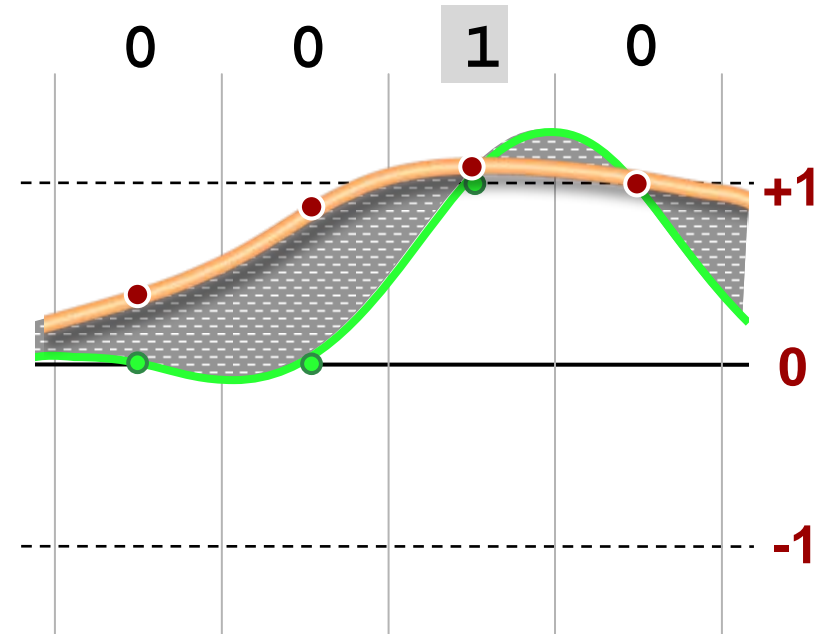
Part 4

The Impact of the Noise Increases in High-Density Environments

LOW DATA DENSITY



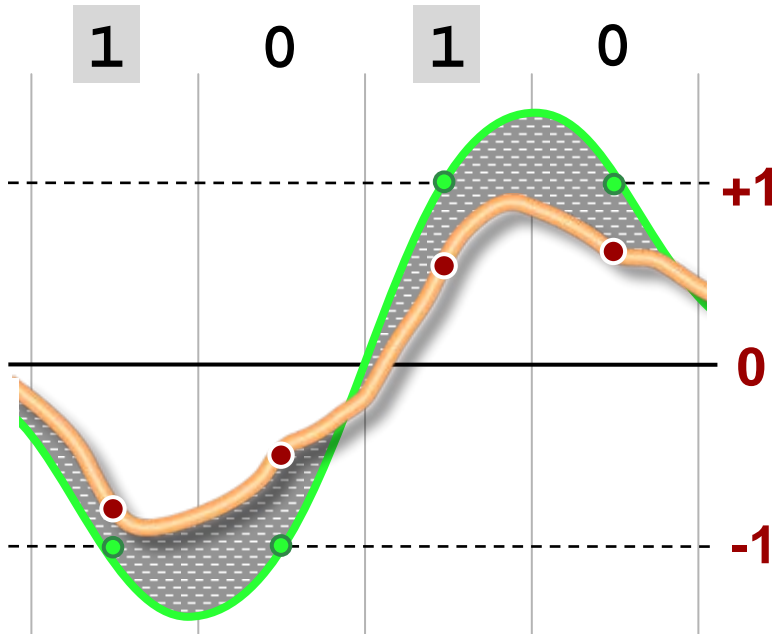
HIGH DATA DENSITY



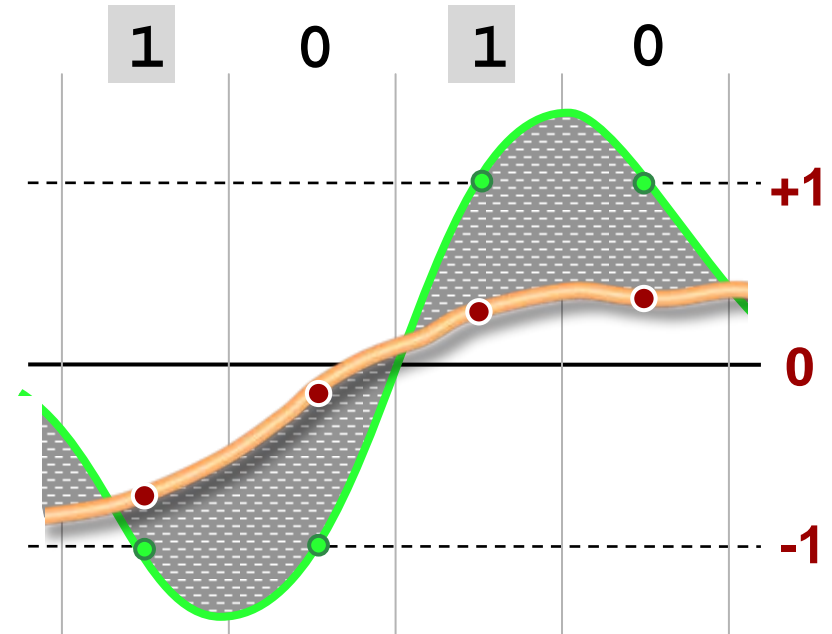
-  Hypothetical "Noise-Free" Signal for this bit pattern
-  Actual Readback Signal generated by the Read Head
-  Noise

The Impact of the Noise Increases in High-Density Environments

LOW DATA DENSITY



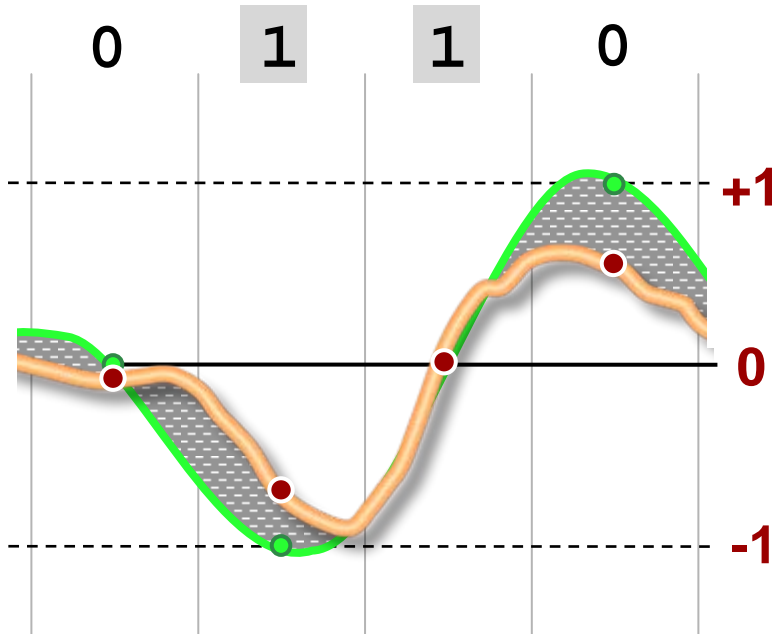
HIGH DATA DENSITY



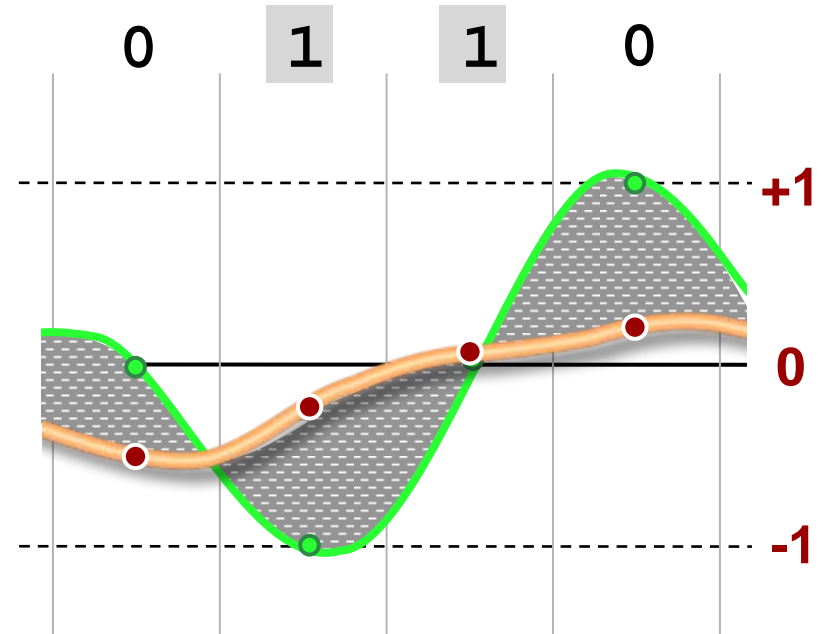
-  Hypothetical "Noise-Free" Signal for this bit pattern
-  Actual Readback Signal generated by the Read Head
-  Noise

The Impact of the Noise Increases in High-Density Environments

LOW DATA DENSITY



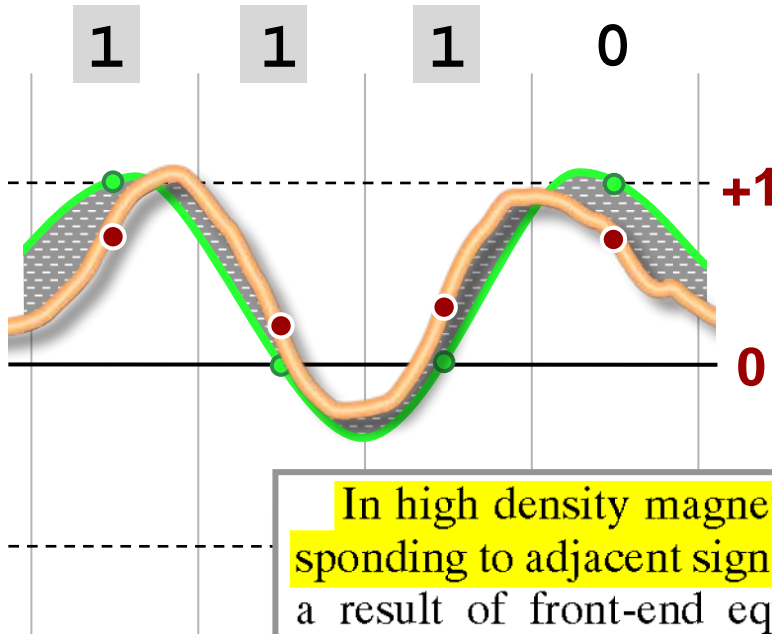
HIGH DATA DENSITY



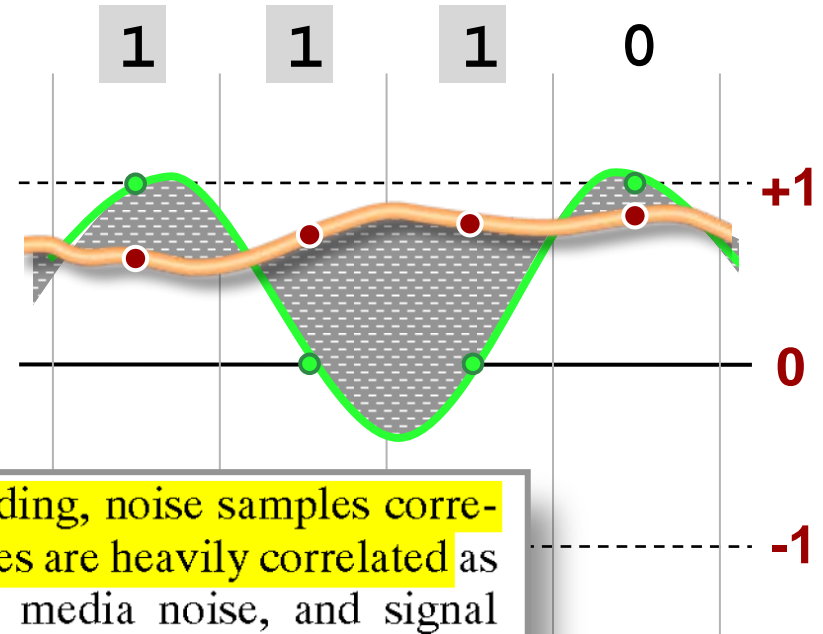
-  Hypothetical "Noise-Free" Signal for this bit pattern
-  Actual Readback Signal generated by the Read Head
-  Noise

The Impact of the Noise Increases in High-Density Environments

LOW DATA DENSITY



HIGH DATA DENSITY

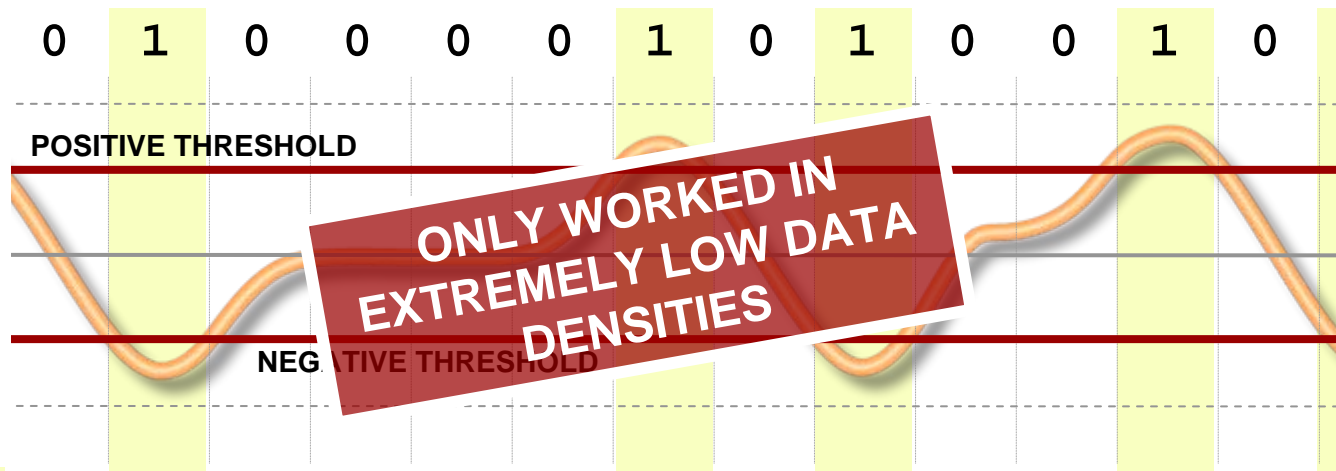


In high density magnetic recording, noise samples corresponding to adjacent signal samples are heavily correlated as a result of front-end equalizers, media noise, and signal nonlinearities combined with nonlinear filters to cancel them. This correlation deteriorates significantly the performance of detectors at high densities.

-  Hypothetical "Noise-Free" Signal for this bit pattern
-  Actual Readback Signal generated by the Read Head
-  Noise

The Viterbi Algorithm and the “Trellis”

Peak Detectors



Any signal reading above or below a certain negative or positive threshold value is converted to a digital “1”

The Viterbi Algorithm

0 1 0 0 0 0 1 0 1 0 0 1 0

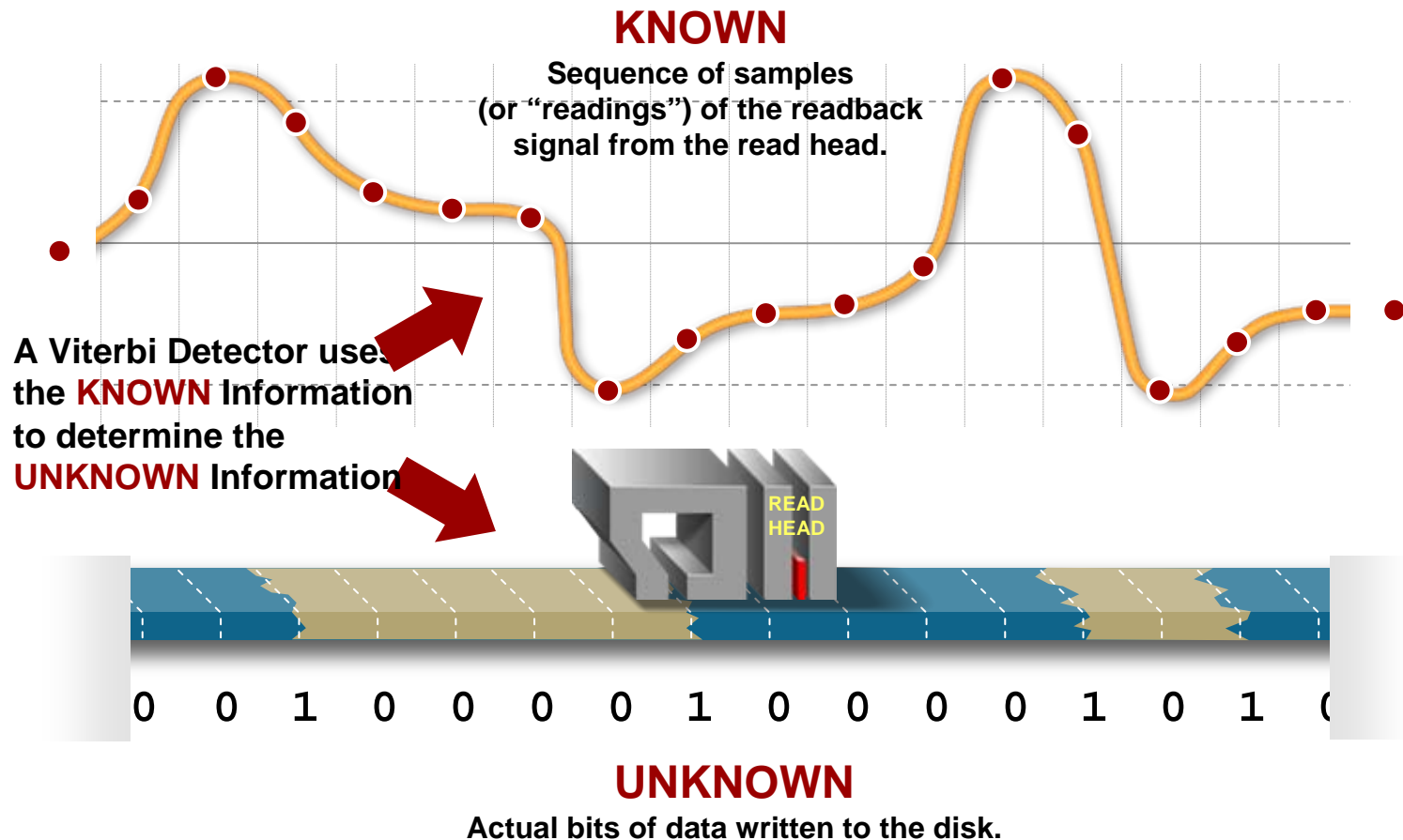


Conceived by Andrew Viterbi in 1967
as a decoding algorithm for noisy
digital communication links
*(used in cell phone signals, satellite
and deep space communication,
speech recognition, Wi-Fi and more)*

Any signal reading above or below a certain
negative or positive threshold value is
converted to a digital “1”

al·go·rithm: a rule (or set of rules) specifying how to solve some problem

“Known” and “Unknown” Information



Data Symbols



on a magnetic medium. The symbols a_i , $i=1, \dots, N$, are drawn from an alphabet of four symbols, $a_i \in \{+, \oplus, -, \ominus\}$. The symbols '+' and '-' denote a positive and a negative transition, respectively. The symbol ' \oplus ' denotes a written zero (no transition) whose nearest preceding non-zero symbol is a '+' while ' \ominus ' denotes a written zero whose nearest preceding transition is a negative one, i.e., '-'. This notation

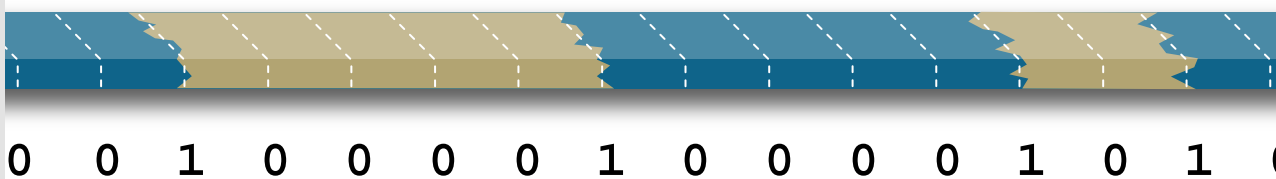
FOUR possible "states"

+

\oplus

\ominus

-



UNKNOWN

Actual bits of data written to the disk.

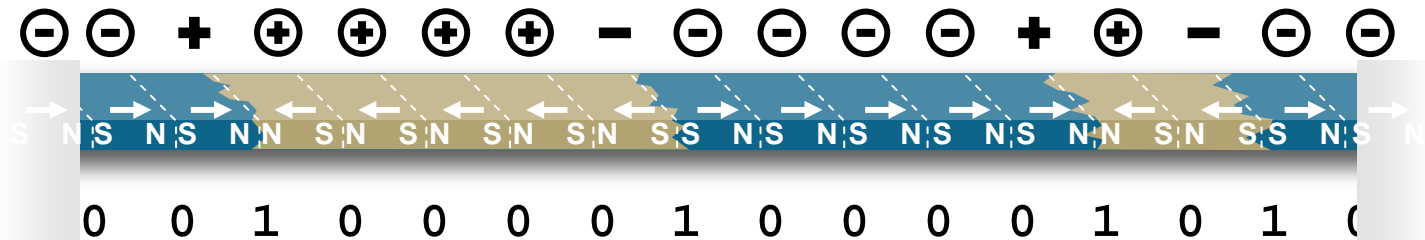
Data Symbols



on a magnetic medium. The symbols a_i , $i=1, \dots, N$, are drawn from an alphabet of four symbols, $a_i \in \{+, \oplus, -, \ominus\}$. The symbols '+' and '-' denote a positive and a negative transition, respectively. The symbol ' \oplus ' denotes a written zero (no transition) whose nearest preceding non-zero symbol is a '+' while ' \ominus ' denotes a written zero whose nearest preceding transition is a negative one, i.e., '-'. This notation

FOUR possible "states"

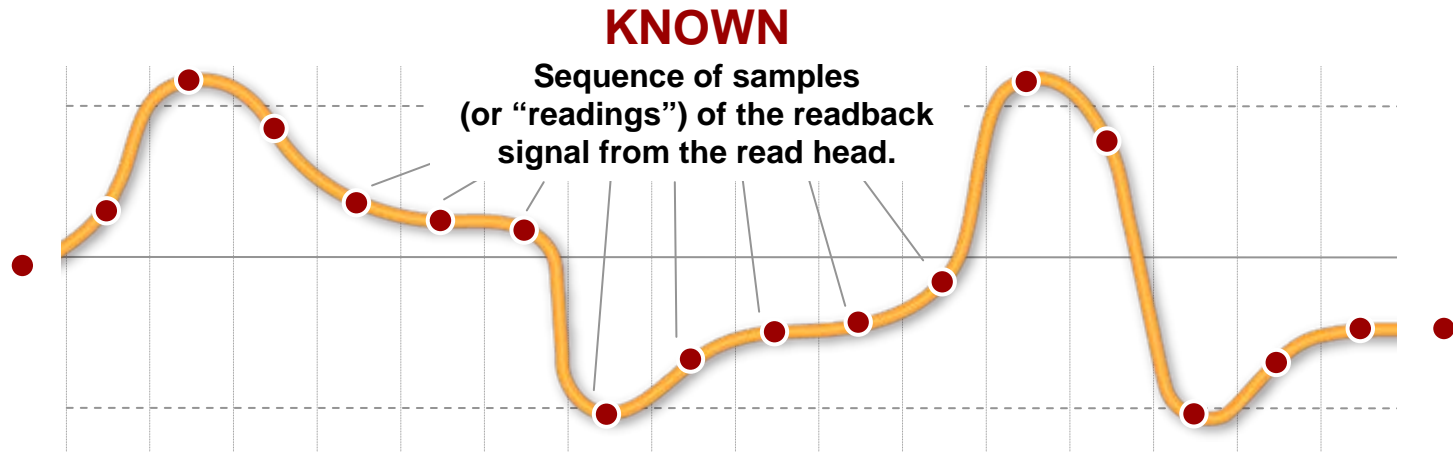
- +** POSITIVE transition
- \oplus** Nearest preceding transition is POSITIVE
- \ominus** Nearest preceding transition is NEGATIVE
- NEGATIVE transition



UNKNOWN

Actual bits of data written to the disk.

Data Symbols



The Trellis

+

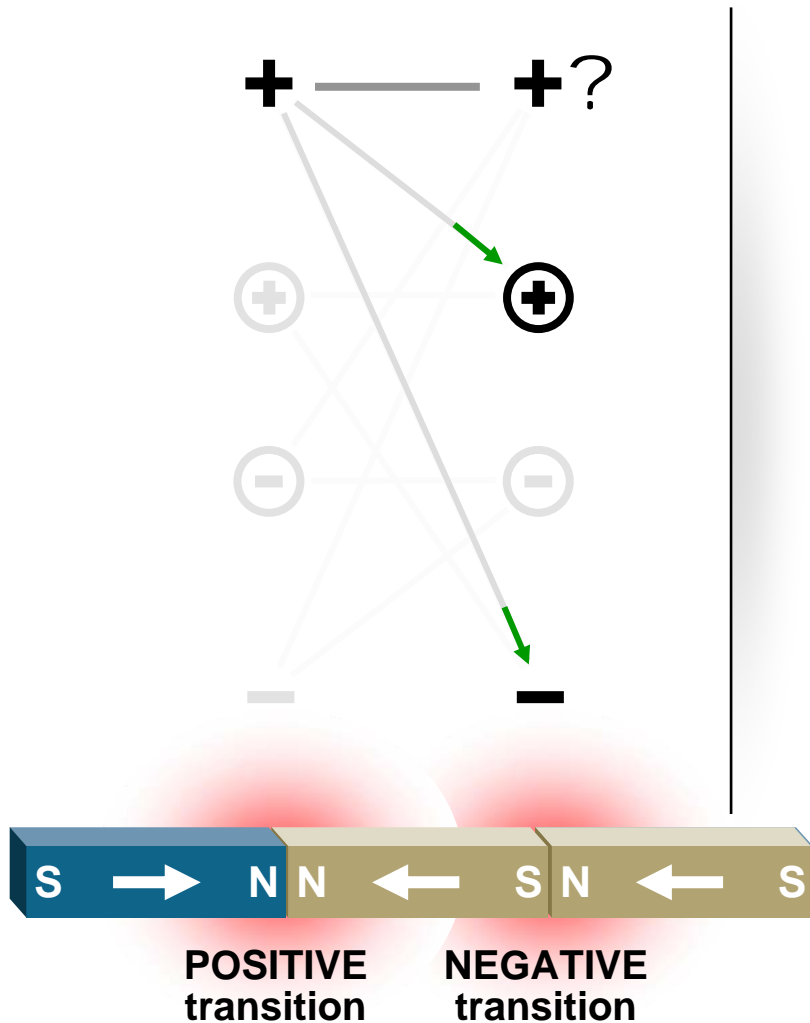
⊕

⊖

—

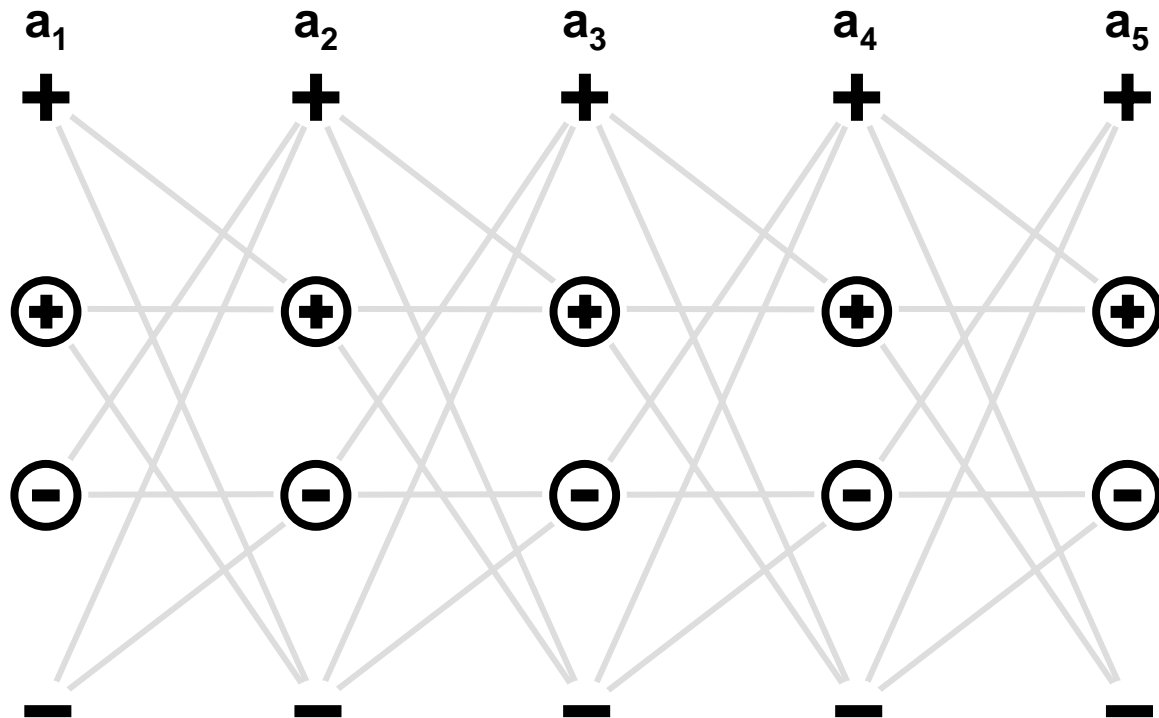
Four possible states for each
symbol written on the disk
(**UNKNOWN** information)

The Trellis

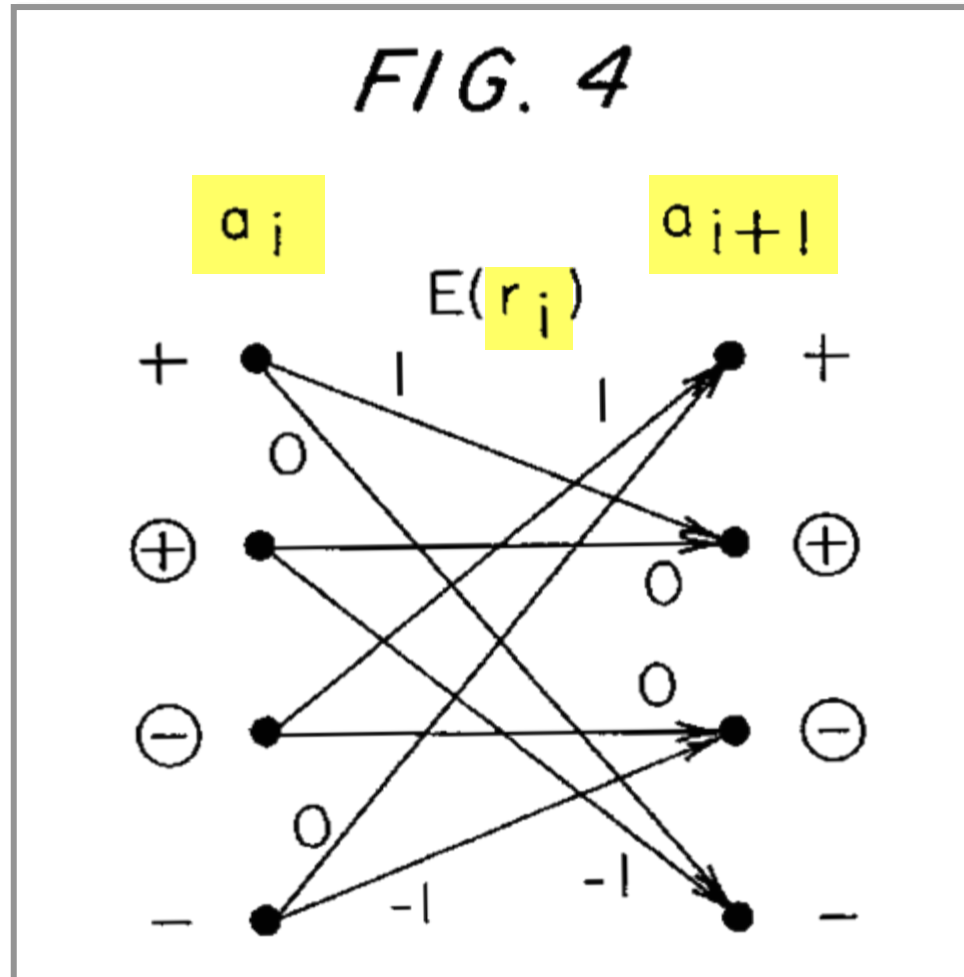
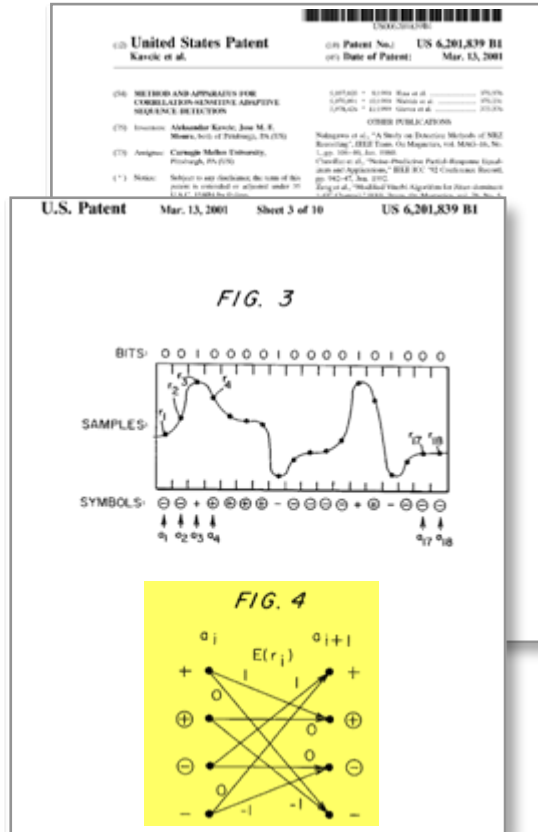


There are two possible connections (or “branches”) coming from and going to each state

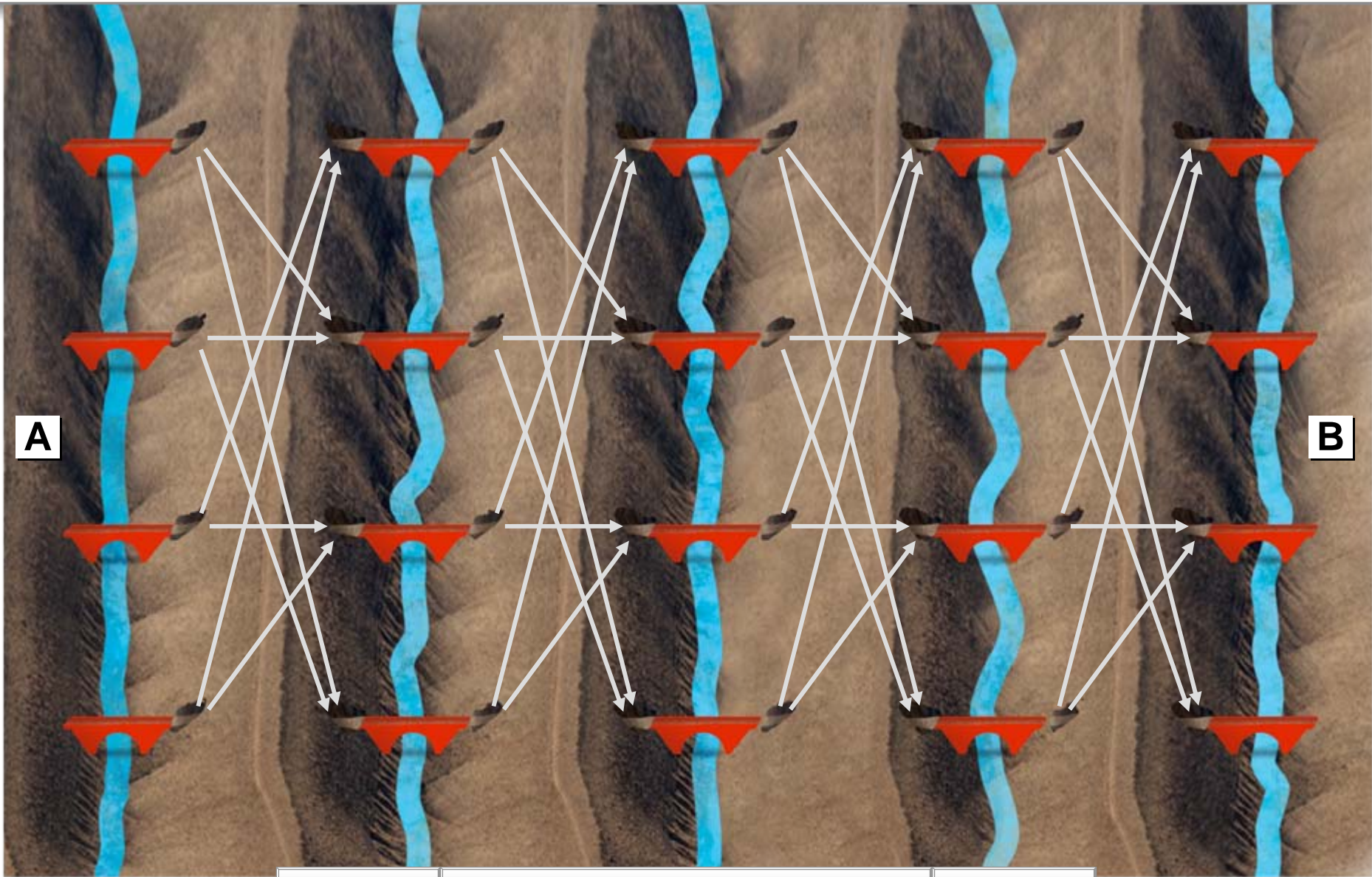
The Trellis



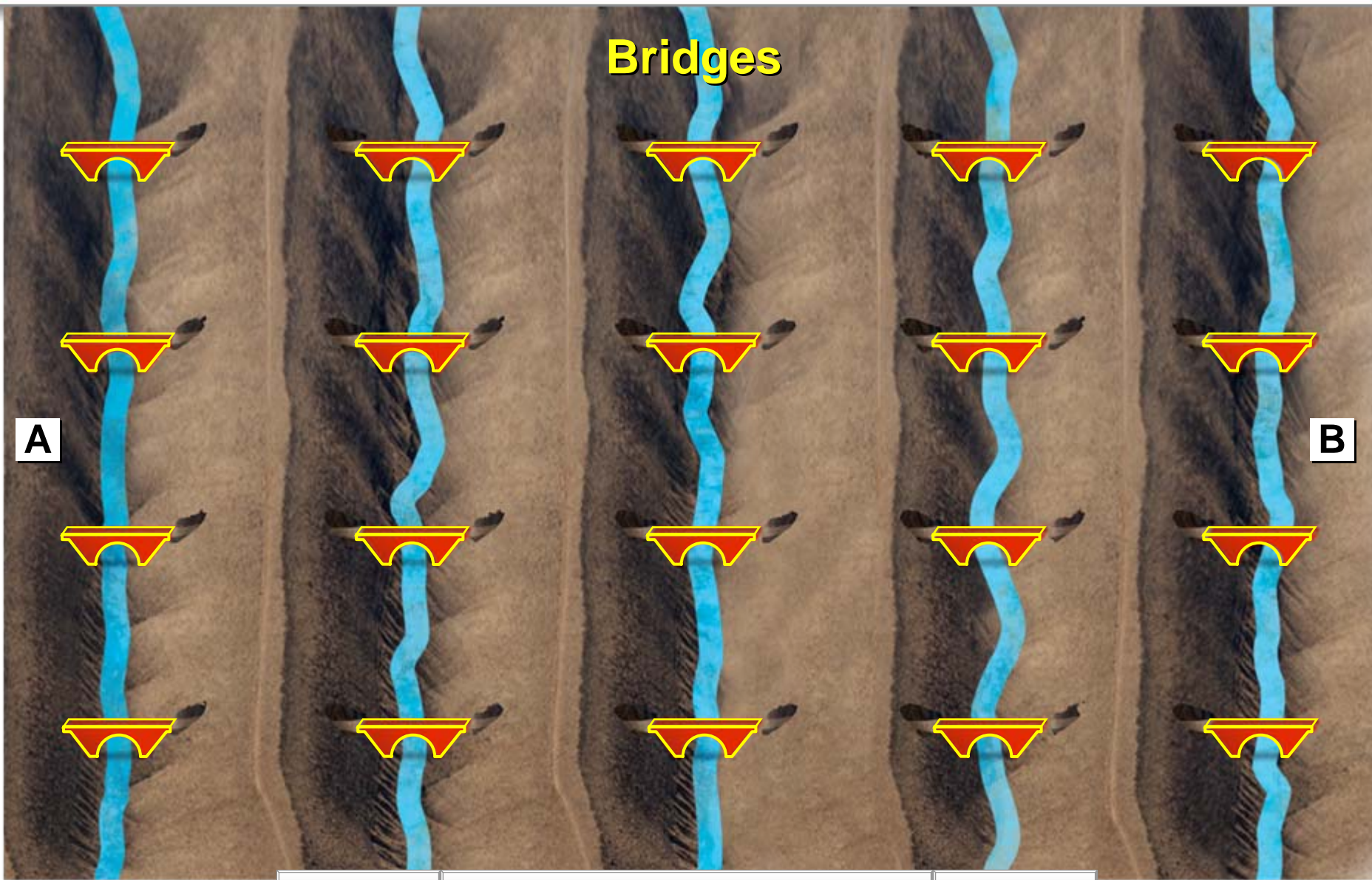
The Kavcic-Moura Patents



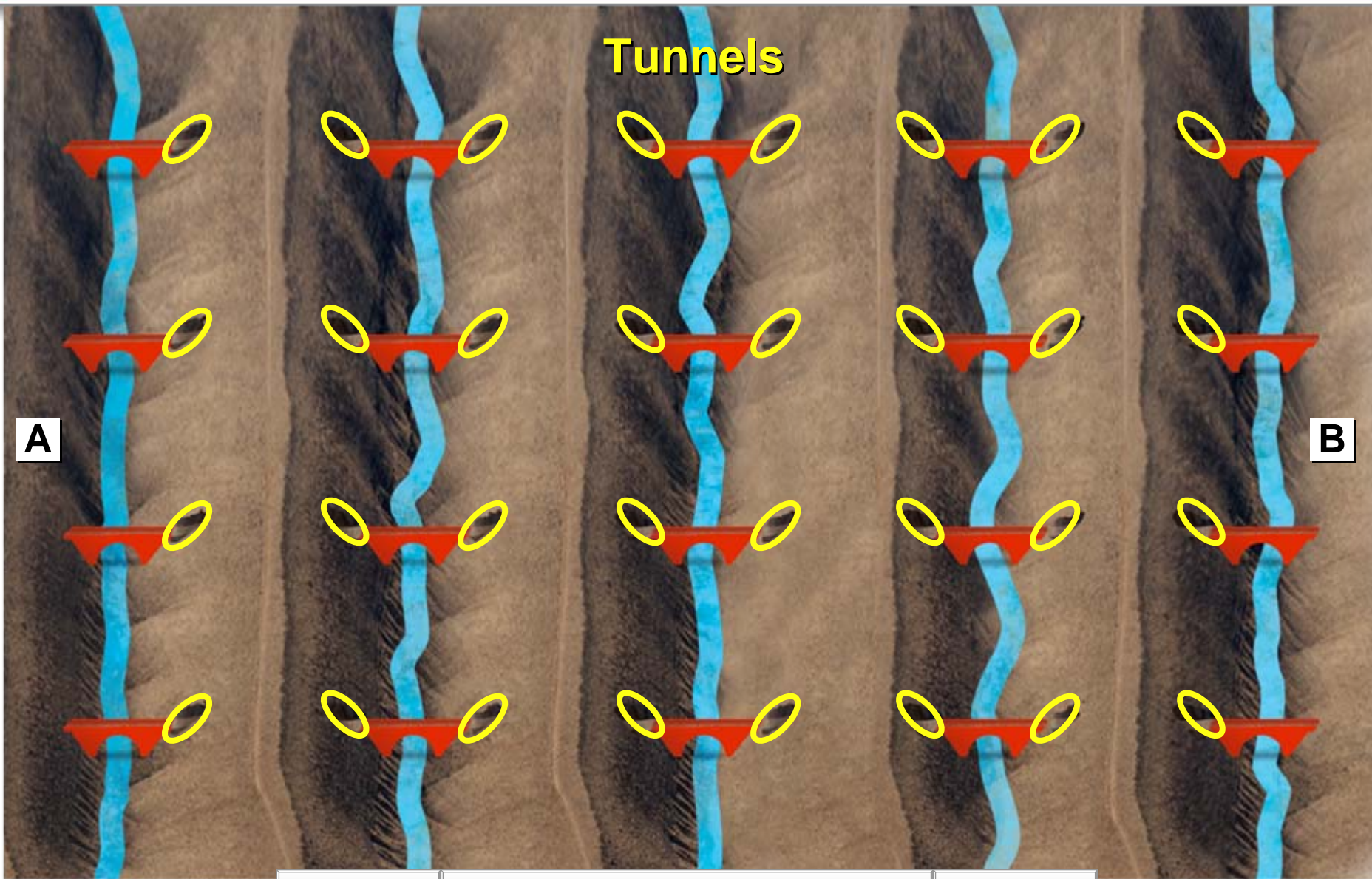
Finding the Most Likely Path from “A” to “B”



Finding the Most Likely Path from “A” to “B”

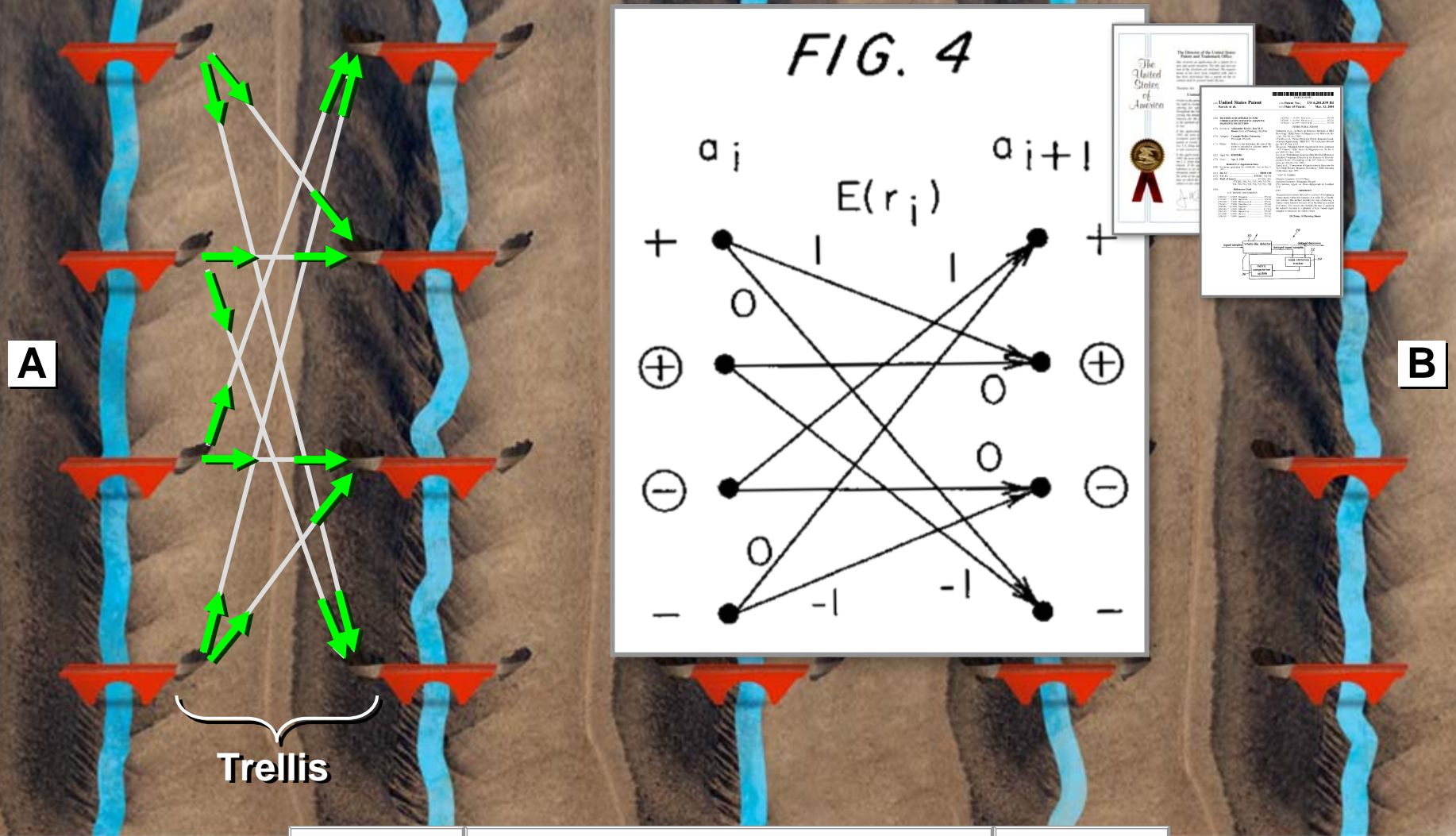


Finding the Most Likely Path from “A” to “B”



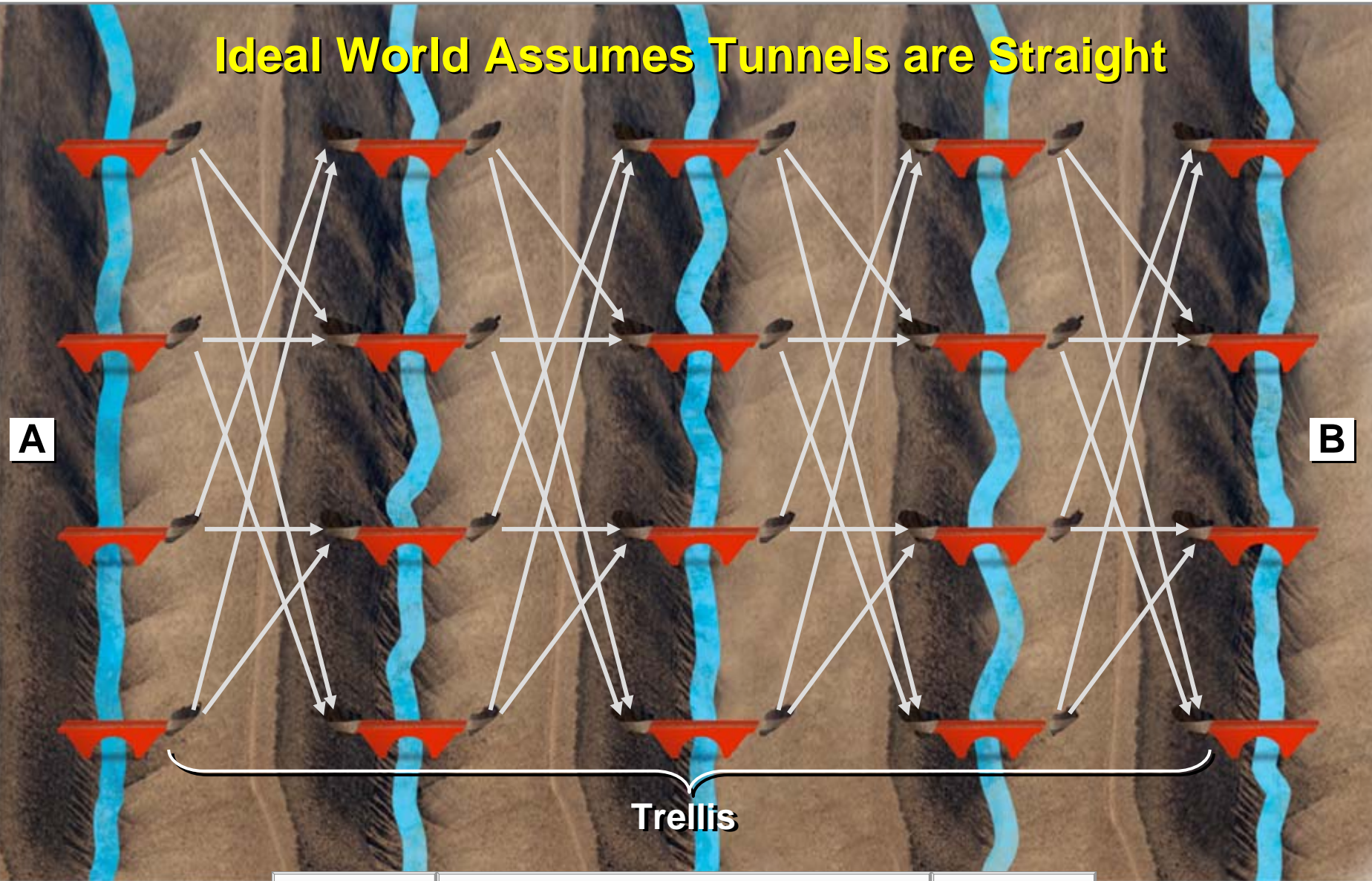
Finding the Most Likely Path from “A” to “B”

Ideal World Assumes Tunnels are Straight



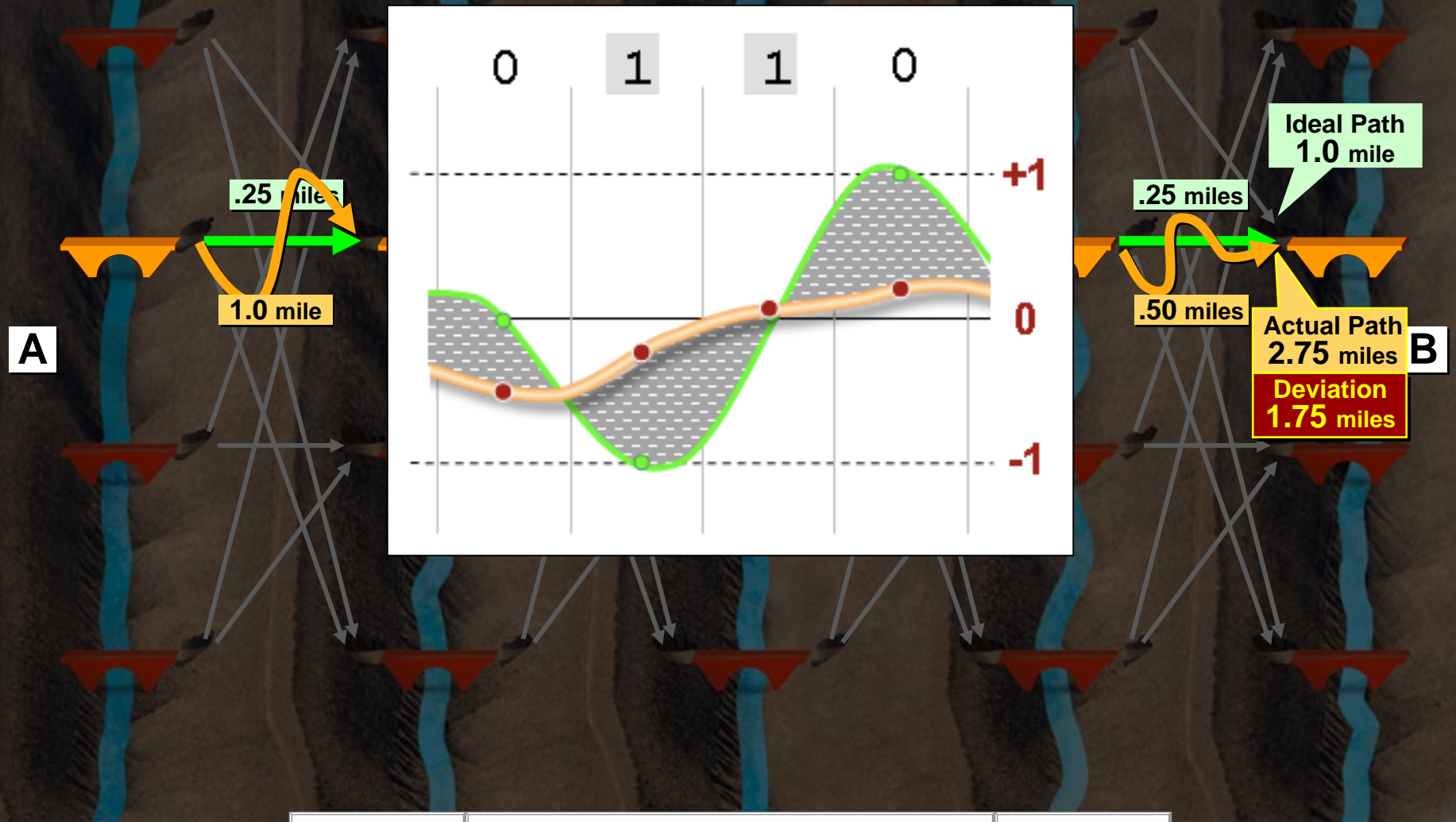
Finding the Most Likely Path from “A” to “B”

Ideal World Assumes Tunnels are Straight



Finding the Most Likely Path from “A” to “B”

Determining the Path with the Least Deviation



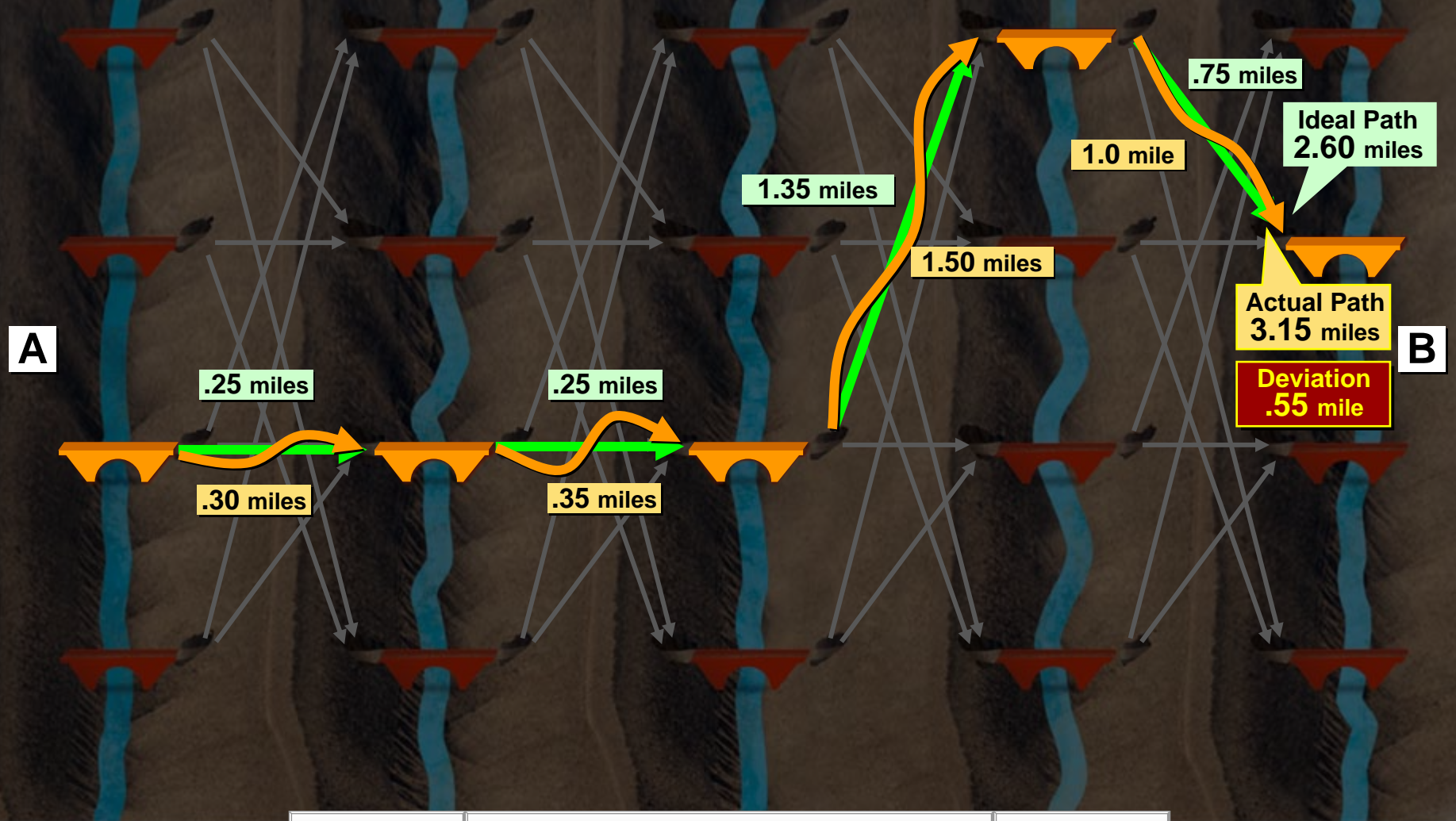
Finding the Most Likely Path from “A” to “B”

Determining the Path with the Least Deviation

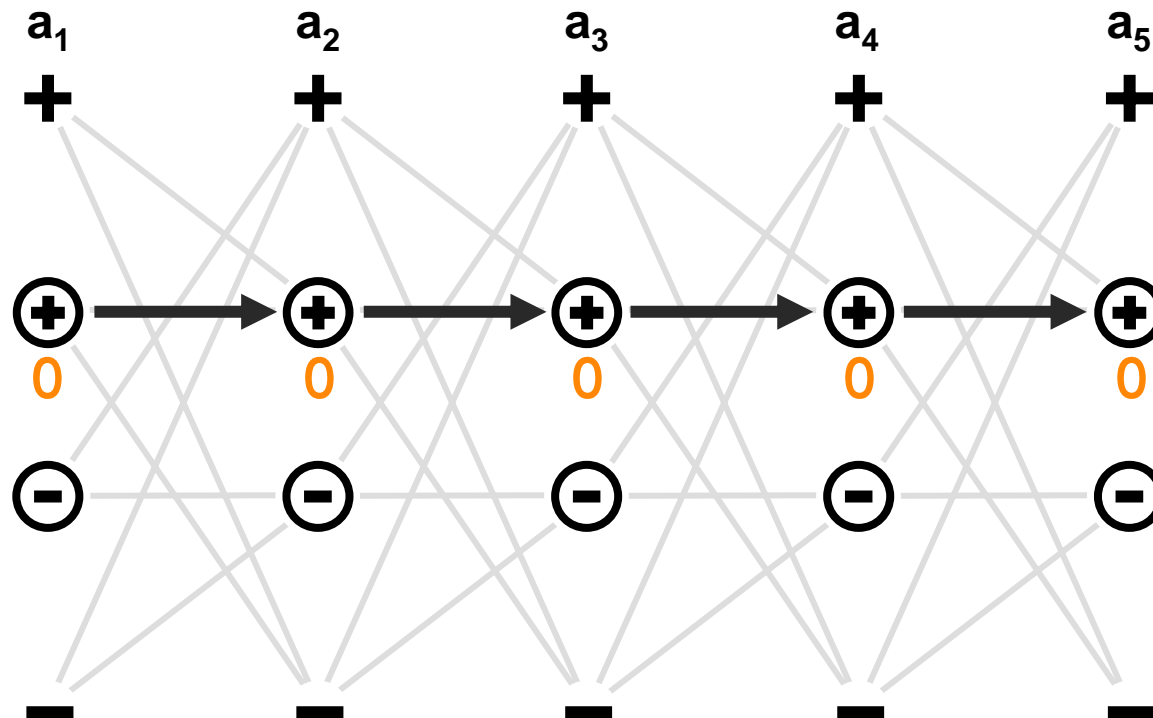


Finding the Most Likely Path from “A” to “B”

Determining Most Likely Paths

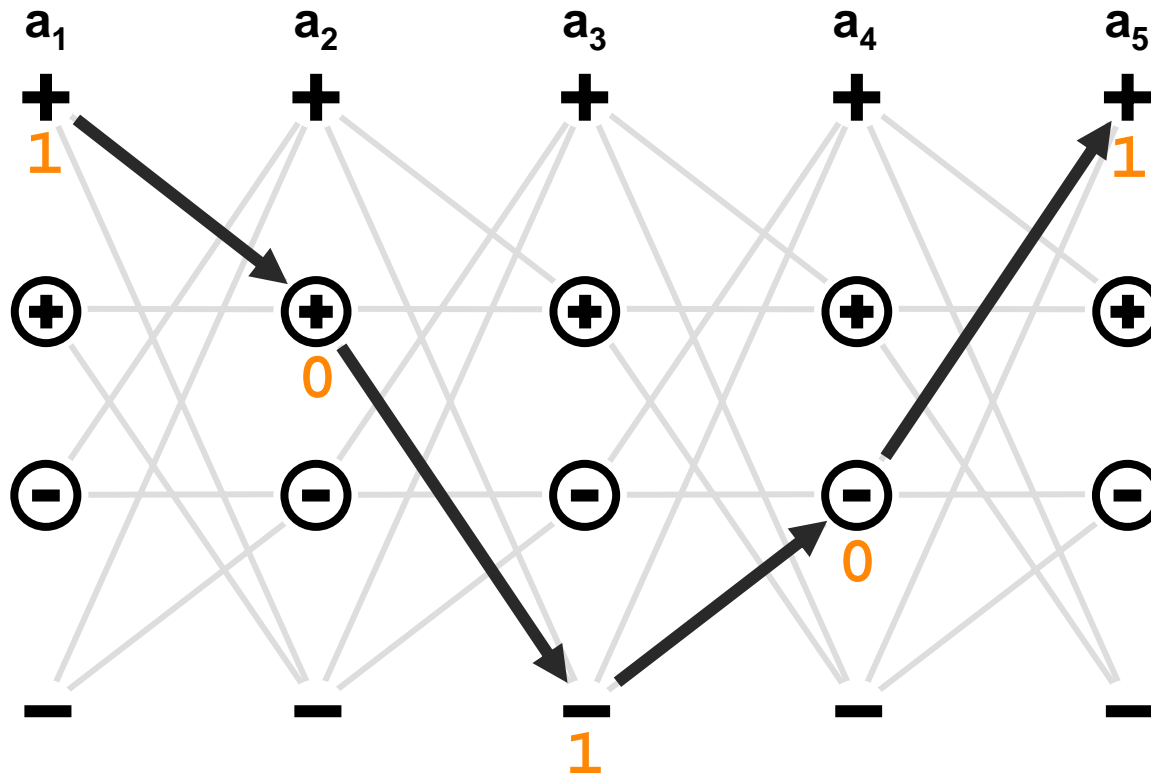


The Trellis



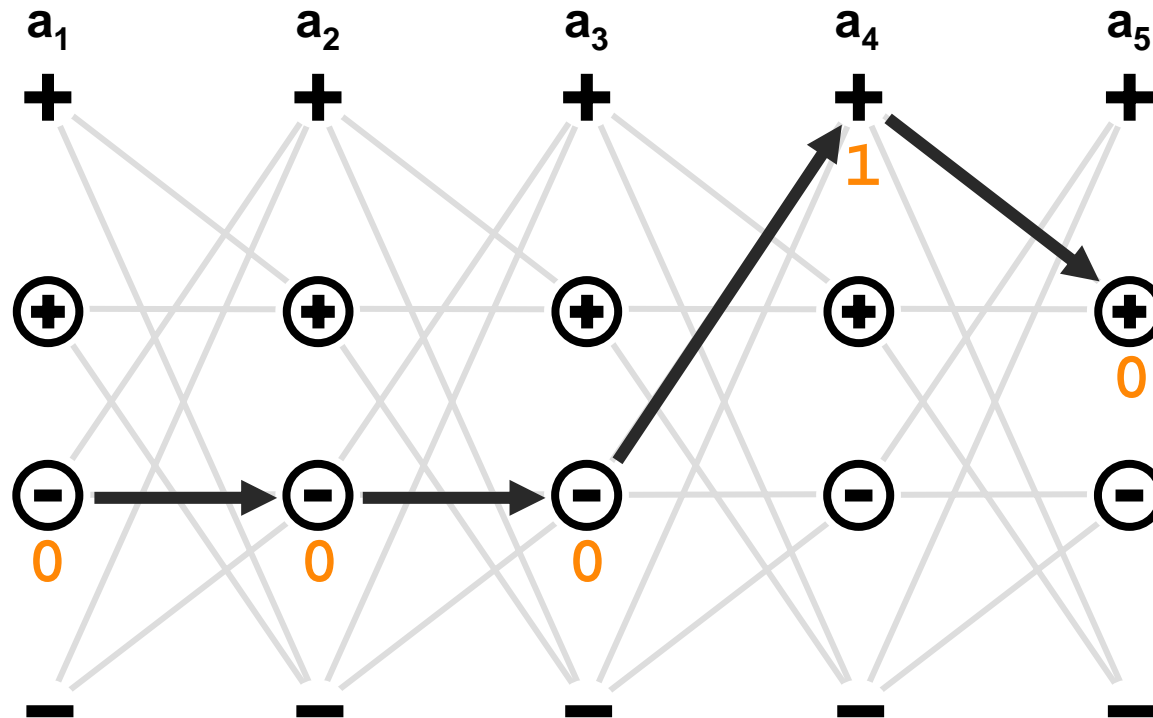
There are numerous possible paths through the trellis

The Trellis



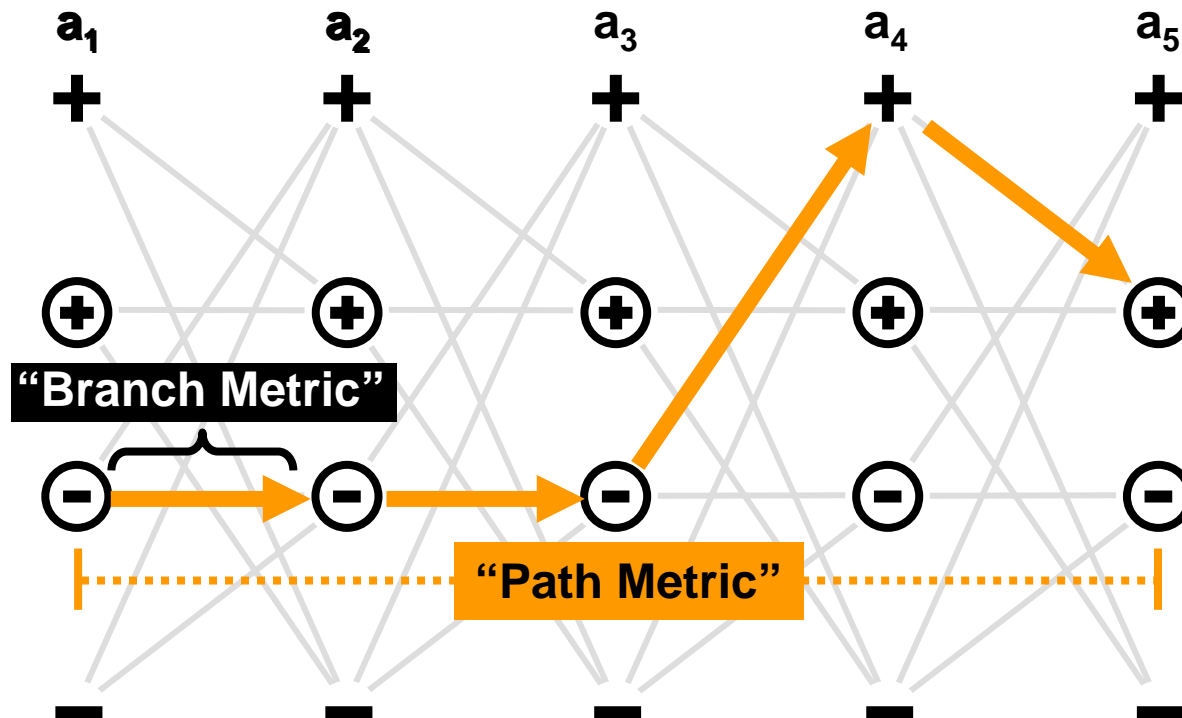
There are numerous possible
paths through the trellis

The Trellis



Finding the most likely path through the trellis
will reveal the symbols written on the disk

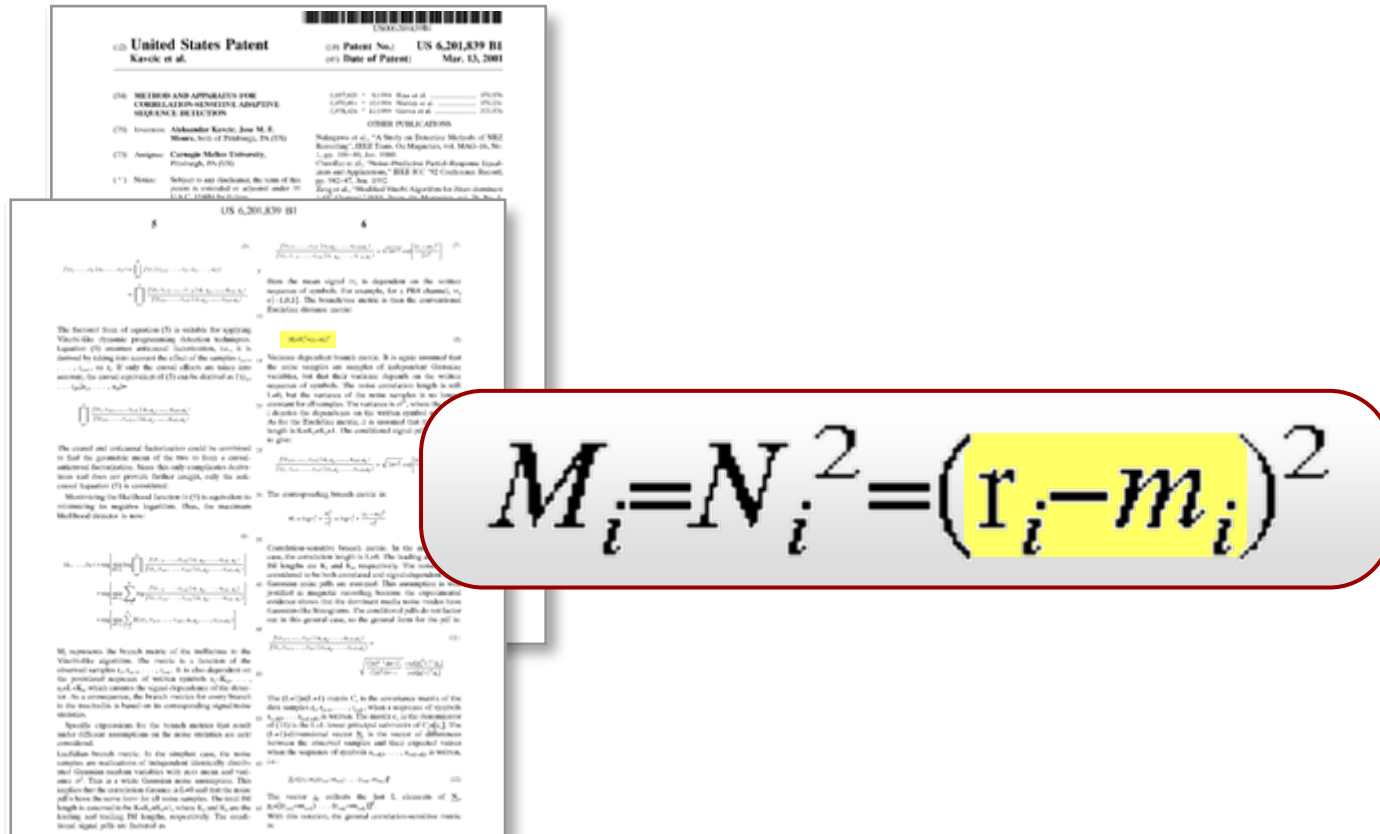
“Branch Metric” and “Path Metric” in the Trellis



Branch Metric Value of Branch between two nodes

Path Metric Sum of separate Branch Metrics

The Kavcic-Moura Patents Describe the Prior Art



Source: '839 Patent
Equation 8 (6:13)

Prior Art Branch Metric Calculation

Readings (r_t) are algorithmically compared to Target Values (m_i) to determine most likely sequence of bits or symbols on the disk

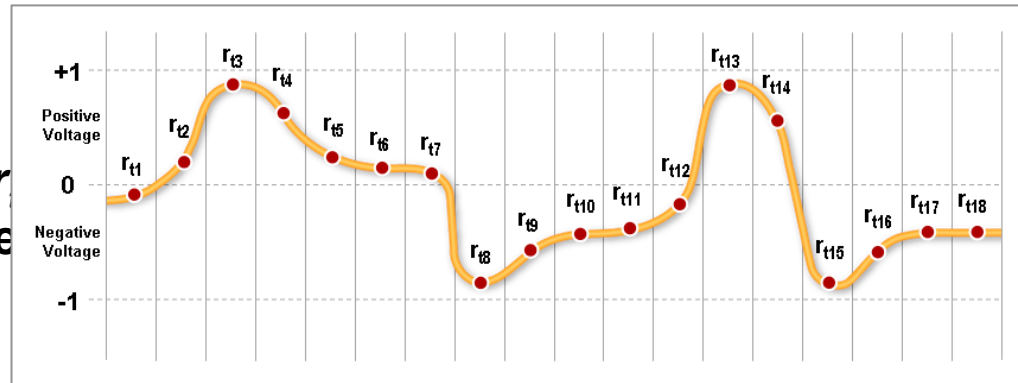
$$BM_i = (r_t - m_i)^2$$

Branch Metric Reading Target Value

The diagram illustrates the formula for Branch Metric Calculation. The formula is enclosed in a rounded rectangle. Below the rectangle, three labels are positioned: 'Branch Metric' under the BM_i , 'Reading' under the r_t , and 'Target Value' under the m_i . Red arrows point upwards from each label to its corresponding variable in the formula.

Prior Art Branch Metric Calculation

Readings (r)
determine



ues (m_i) to
the disk

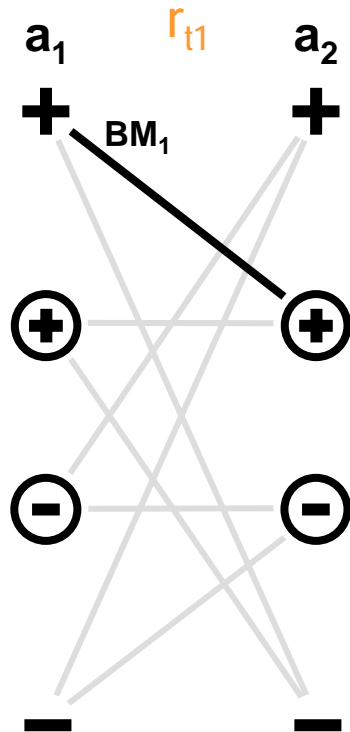
$$BM_i = (r_t - m_i)^2$$

Branch Metric #

Specific Time
Index of Sample

Branch Metric #

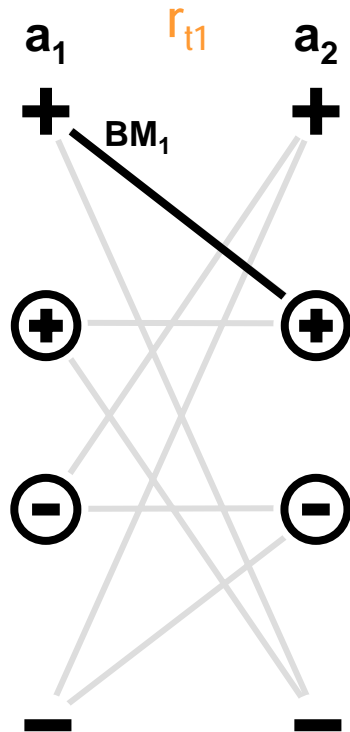
Branch Metrics



Computing Branch Metric 1 (BM_1)

$$BM_i = (r_t - m_i)^2$$

Branch Metrics

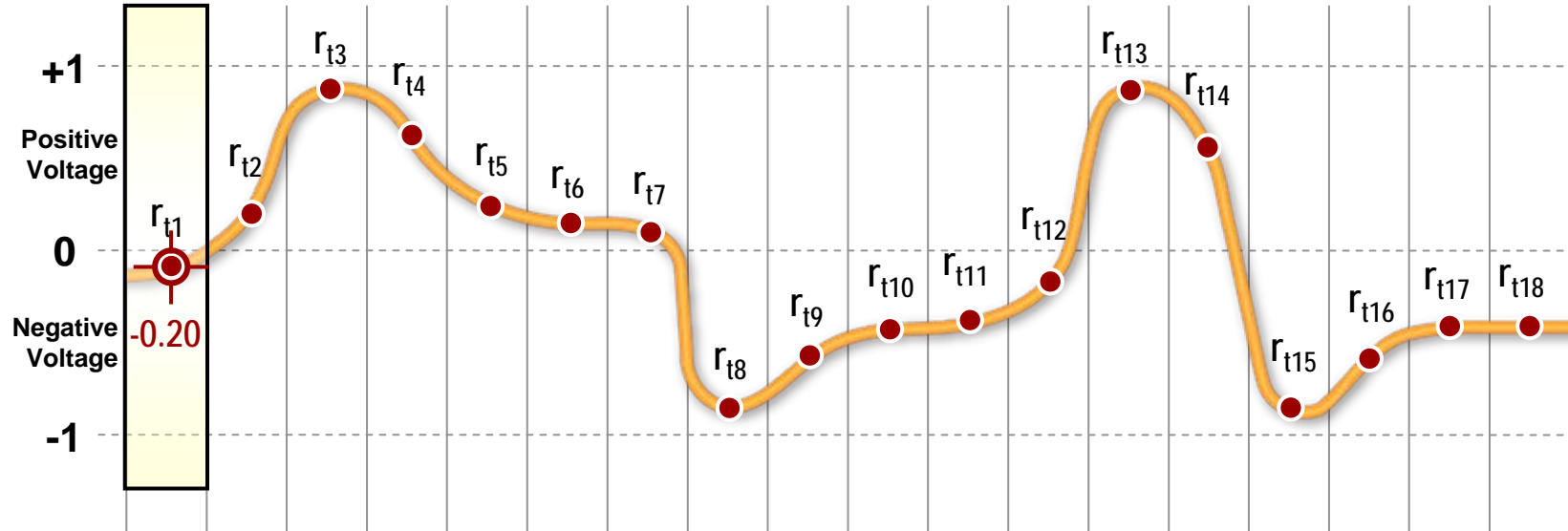


Computing Branch Metric 1 (BM_1)

?

$$BM_1 = (r_{t1} - m_1)^2$$

r-Values are Obtained From Readings Taken at Specific Time Intervals

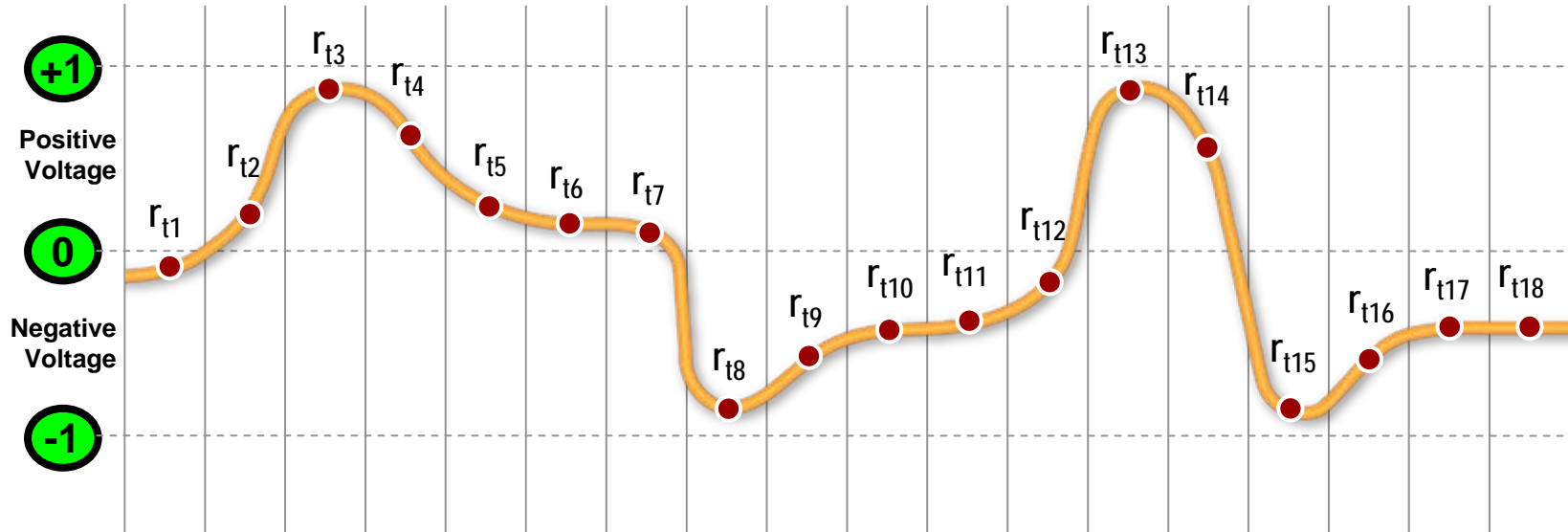


?

$$BM_1 = (\quad - m_1)^2$$

Target Values

Target Values
(m_i)



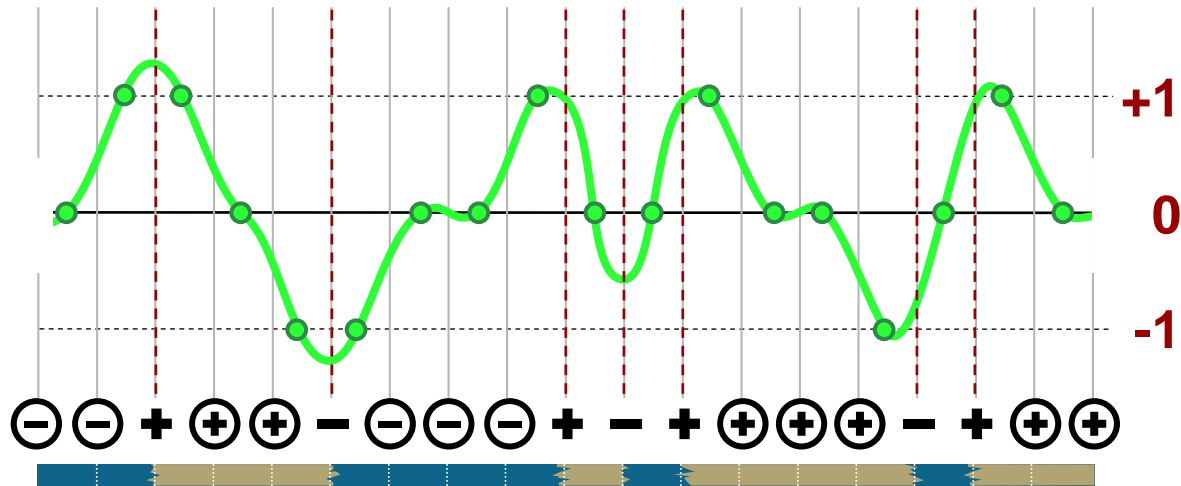
?

$$BM_1 = (-0.20 - m_1)^2$$

Ideal Target Values



Composite Ideal
Target Signal

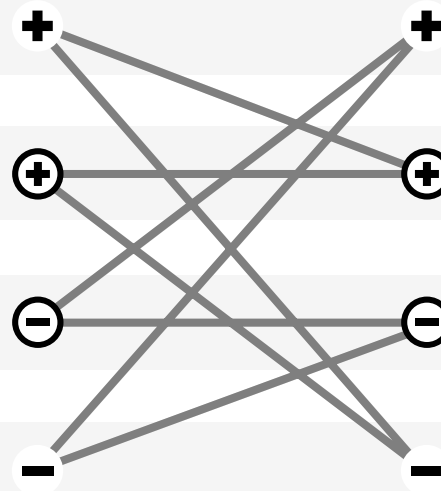


POSITIVE transition

Nearest preceding transition
is **POSITIVE**

Nearest preceding transition
is **NEGATIVE**

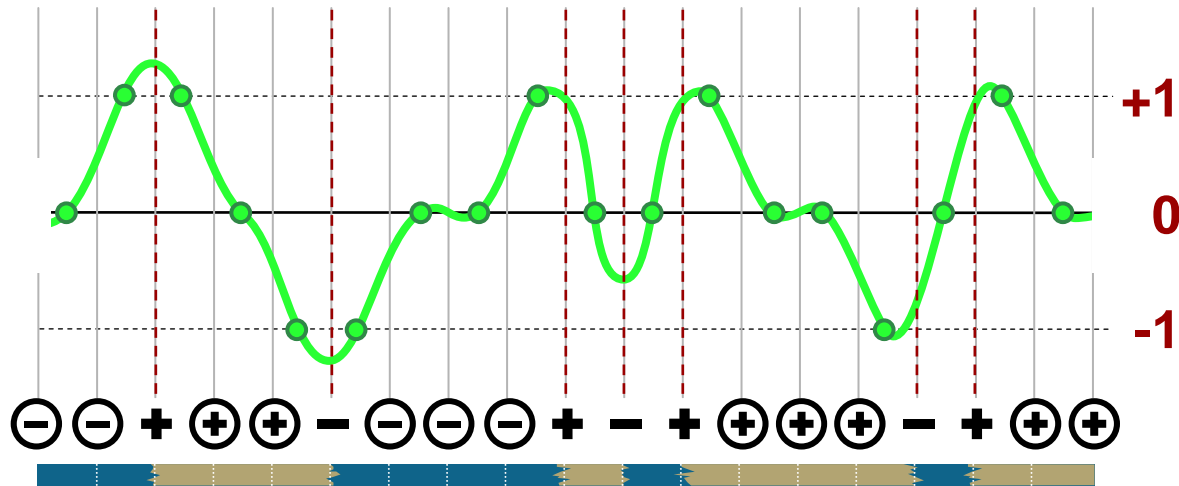
NEGATIVE transition



Ideal Target Values



Composite Ideal
Target Signal



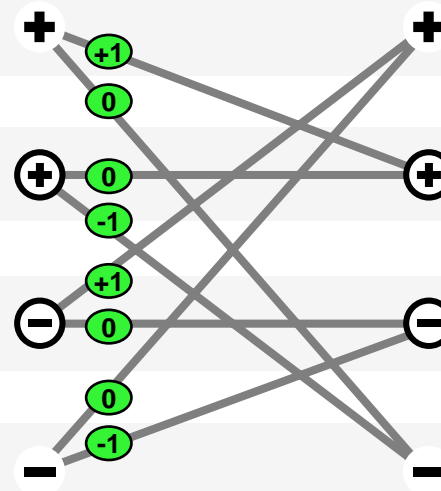
BM8

POSITIVE transition

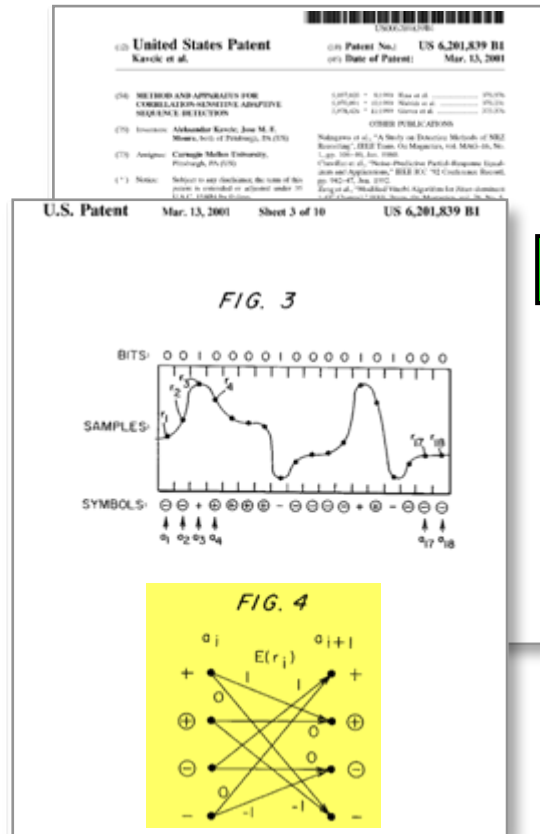
Nearest preceding transition
is **POSITIVE**

Nearest preceding transition
is **NEGATIVE**

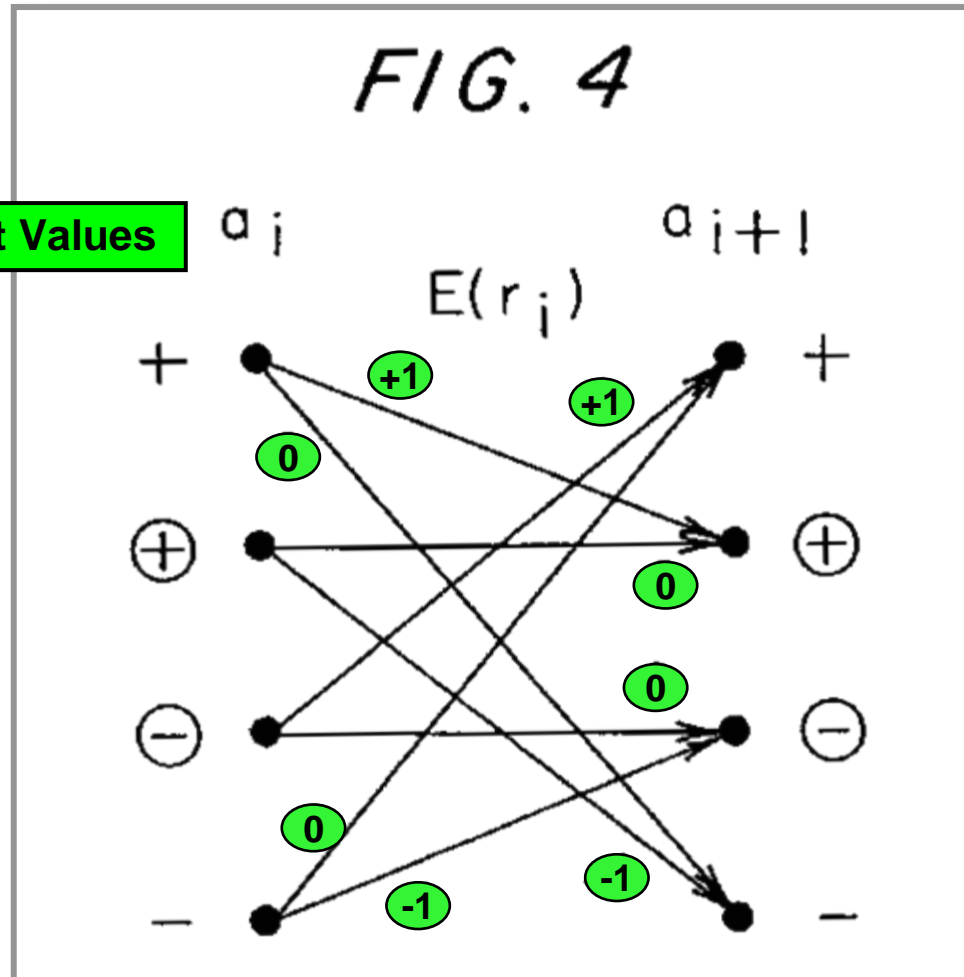
NEGATIVE transition



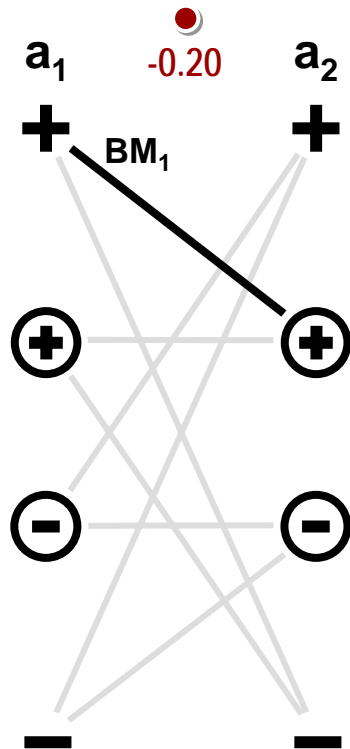
Ideal Target Values in Figure 4



Target Values



Computing Branch Metrics



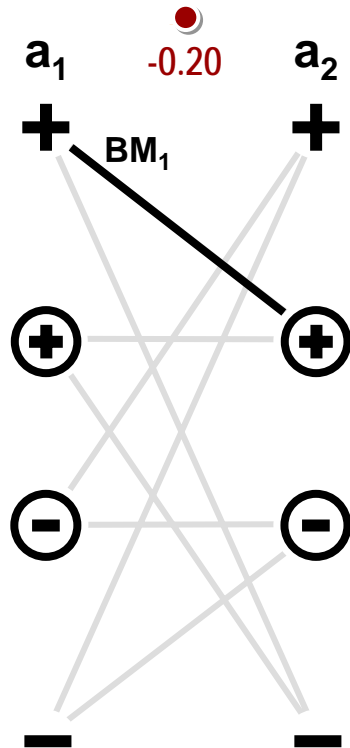
Computing Branch Metric 1 (BM_1)

$$m_1 = +1$$

?

$$BM_1 = (-0.20 - m_1)^2$$

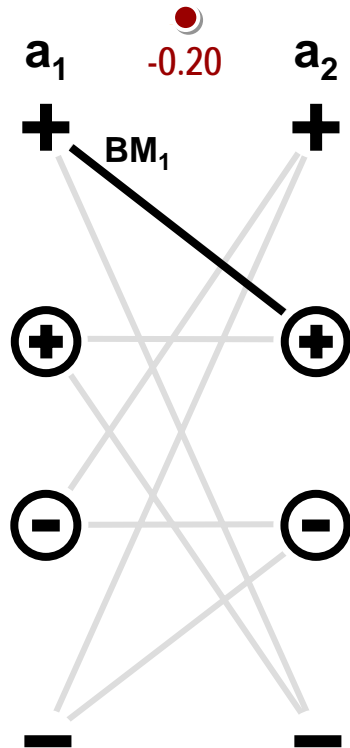
Computing Branch Metrics



Computing Branch Metric 1 (BM_1)

$$BM_1 = (-0.20 - 1)^2$$

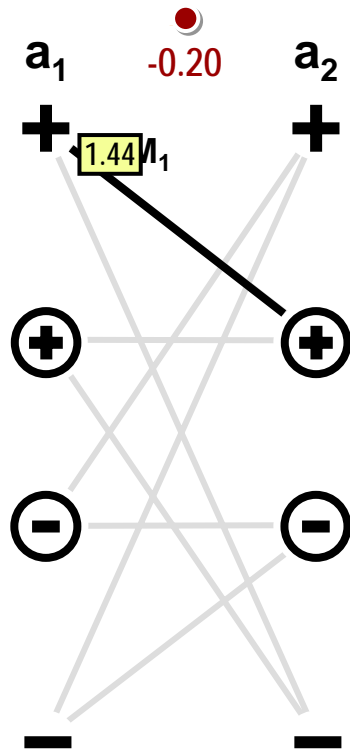
Computing Branch Metrics



Computing Branch Metric 1 (BM_1)

$$BM_1 = (- 1.20)^2$$

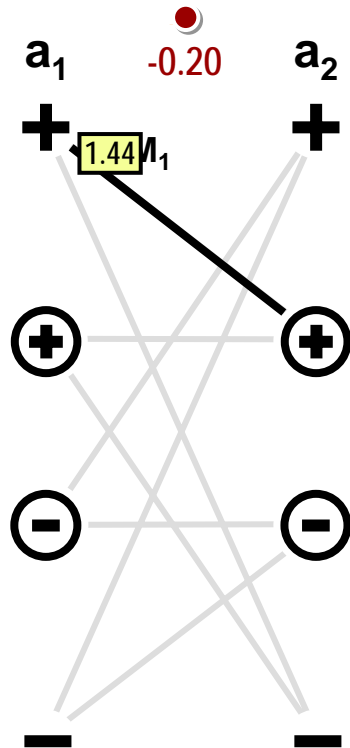
Computing Branch Metrics



Computing Branch Metric 1 (BM_1)

$$BM_1 = 1.44$$

Computing Branch Metrics



$$BM_1 = 1.44$$

$$BM_2 = (r_1 - m_2)^2$$

$$BM_3 = (r_1 - m_3)^2$$

$$BM_4 = (r_1 - m_4)^2$$

$$BM_5 = (r_1 - m_5)^2$$

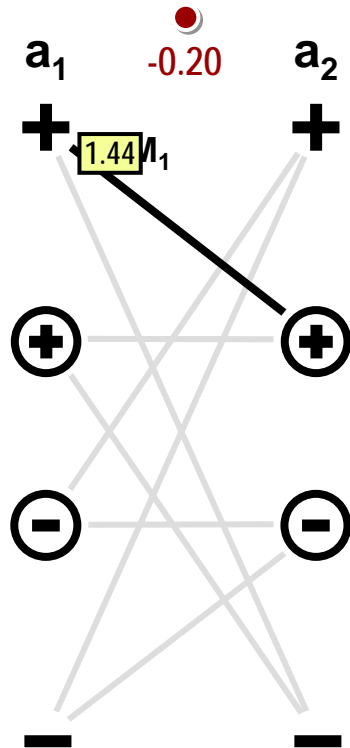
$$BM_6 = (r_1 - m_6)^2$$

$$BM_7 = (r_1 - m_7)^2$$

$$BM_8 = (r_1 - m_8)^2$$

$$BM_i = (r_t - m_i)^2$$

Computing Branch Metrics



$$BM_1 = 1.44$$

$$BM_2 = (r_1 - m_2)^2$$

$$BM_3 = (r_1 - m_3)^2$$

$$BM_4 = (r_1 - m_4)^2$$

$$BM_5 = (r_1 - m_5)^2$$

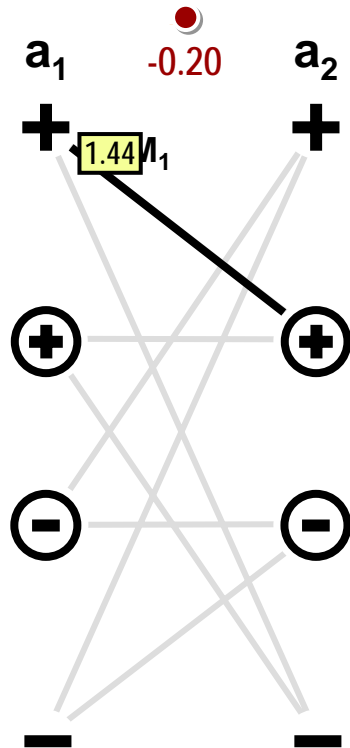
$$BM_6 = (r_1 - m_6)^2$$

$$BM_7 = (r_1 - m_7)^2$$

$$BM_8 = (r_1 - m_8)^2$$

$$BM_i = (r_t - m_i)^2$$

Computing Branch Metrics



$$BM_1 = 1.44$$

$$BM_2 = (-0.20 - m_2)^2$$

$$BM_3 = (-0.20 - m_3)^2$$

$$BM_4 = (-0.20 - m_4)^2$$

$$BM_5 = (-0.20 - m_5)^2$$

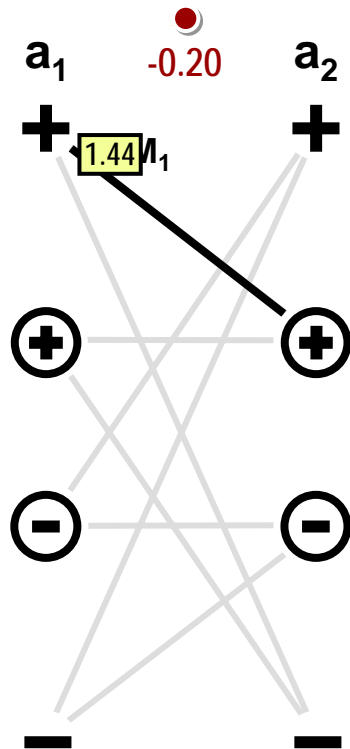
$$BM_6 = (-0.20 - m_6)^2$$

$$BM_7 = (-0.20 - m_7)^2$$

$$BM_8 = (-0.20 - m_8)^2$$

$$BM_i = (r_t - m_i)^2$$

Computing Branch Metrics



$$BM_1 = 1.44$$

$$BM_2 = (-0.20 - m_2)^2$$

$$BM_3 = (-0.20 - m_3)^2$$

$$BM_4 = (-0.20 - m_4)^2$$

$$BM_5 = (-0.20 - m_5)^2$$

$$BM_6 = (-0.20 - m_6)^2$$

$$BM_7 = (-0.20 - m_7)^2$$

$$BM_8 = (-0.20 - m_8)^2$$

$$m_2 = 0$$

$$m_3 = 0$$

$$m_4 = -1$$

$$m_5 = 1$$

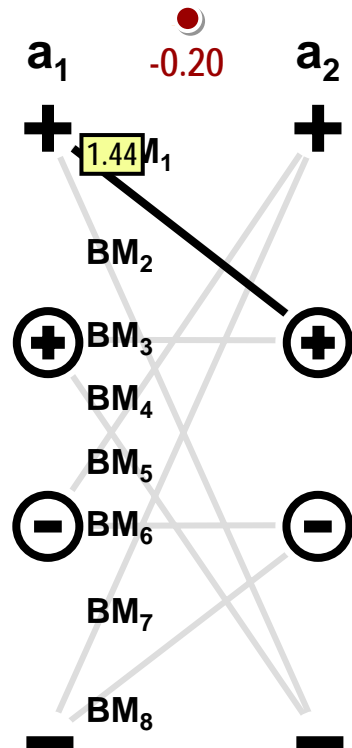
$$m_6 = 0$$

$$m_7 = 0$$

$$m_8 = -1$$

$$BM_i = (r_t - m_i)^2$$

Computing Branch Metrics



$$BM_1 = 1.44$$

$$BM_2 = (-0.20 - 0)^2$$

$$BM_3 = (-0.20 - 0)^2$$

$$BM_4 = (-0.20 - -1)^2$$

$$BM_5 = (-0.20 - 1)^2$$

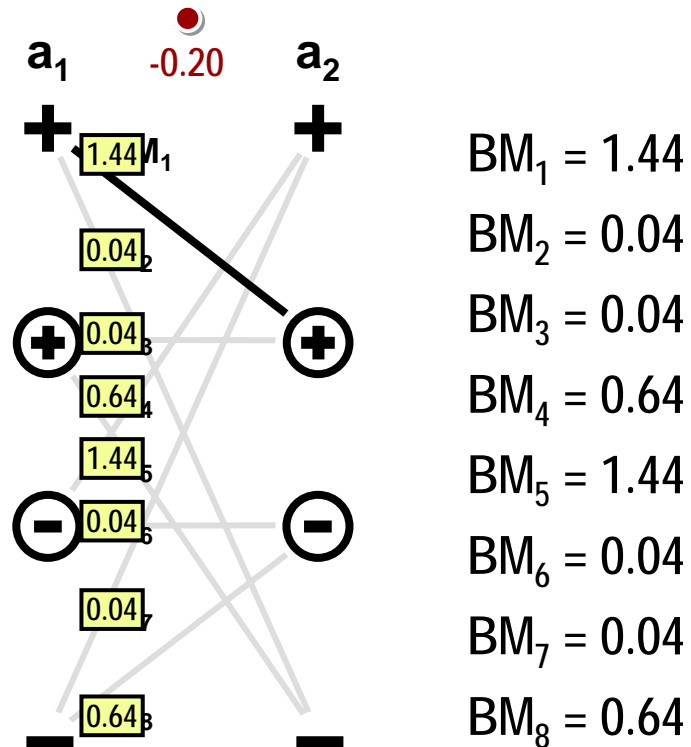
$$BM_6 = (-0.20 - 0)^2$$

$$BM_7 = (-0.20 - 0)^2$$

$$BM_8 = (-0.20 - -1)^2$$

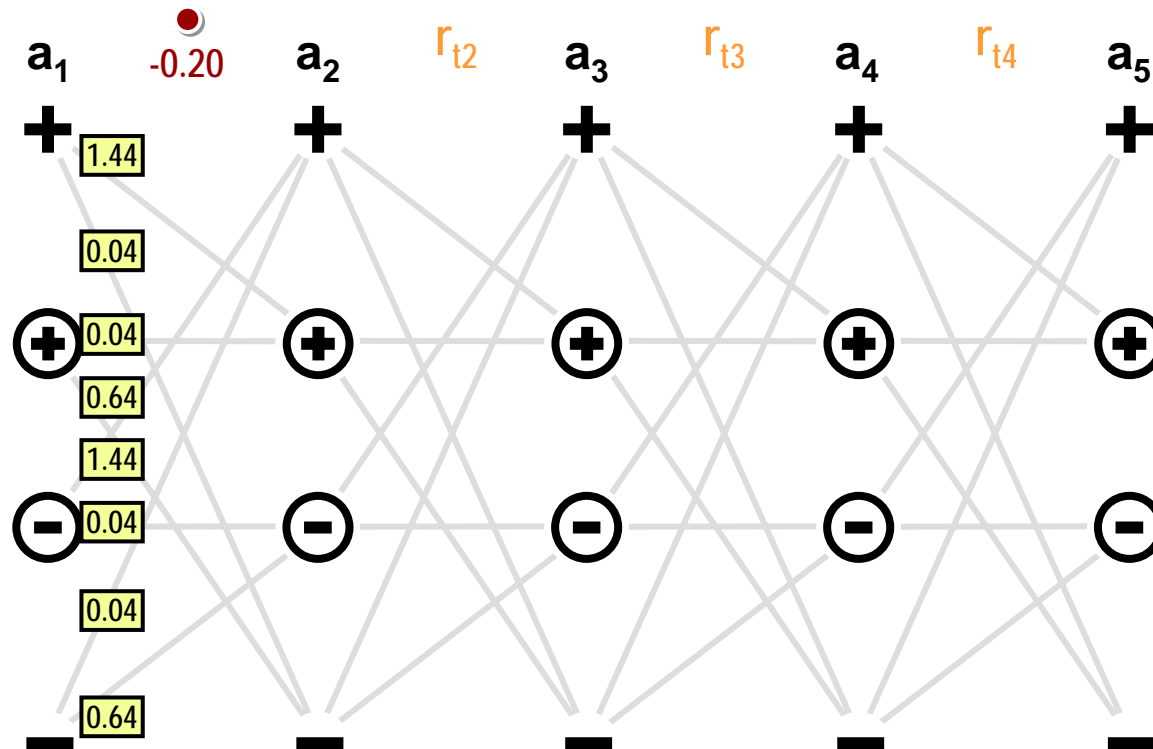
$$BM_i = (r_t - m_i)^2$$

Computing Branch Metrics



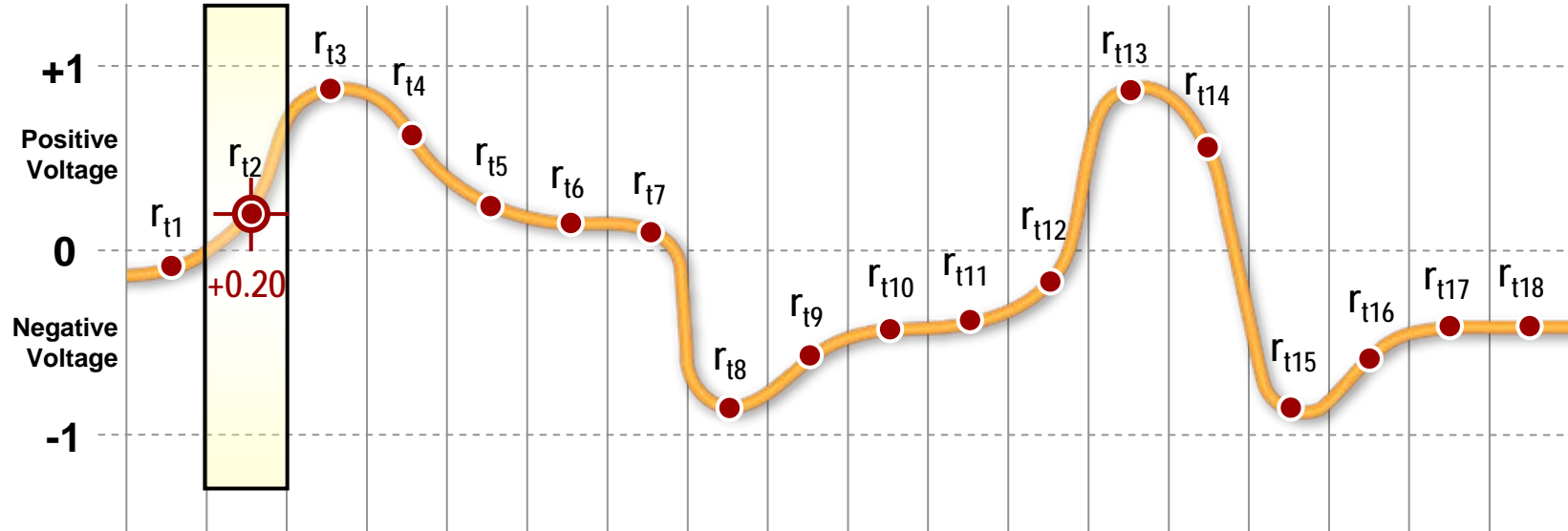
$$BM_i = (r_t - m_i)^2$$

Computing Branch Metrics



$$BM_i = (r_t - m_i)^2$$

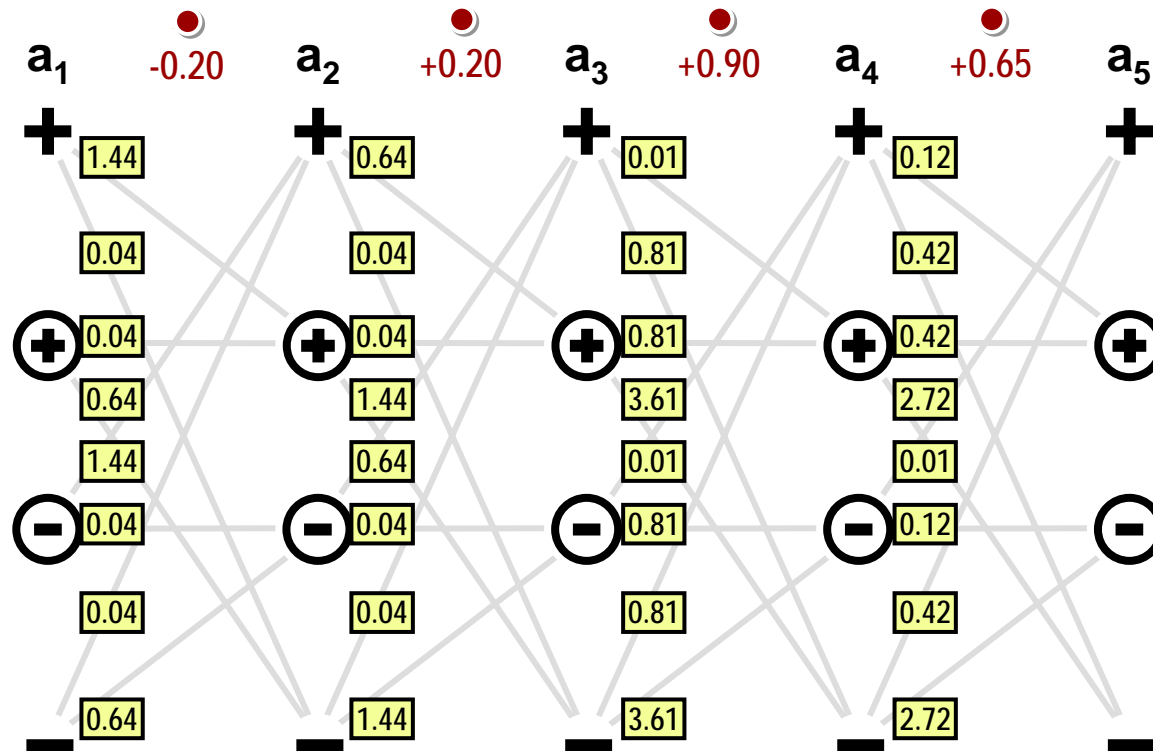
r-Values are Obtained From Readings Taken at Specific Time Intervals



?

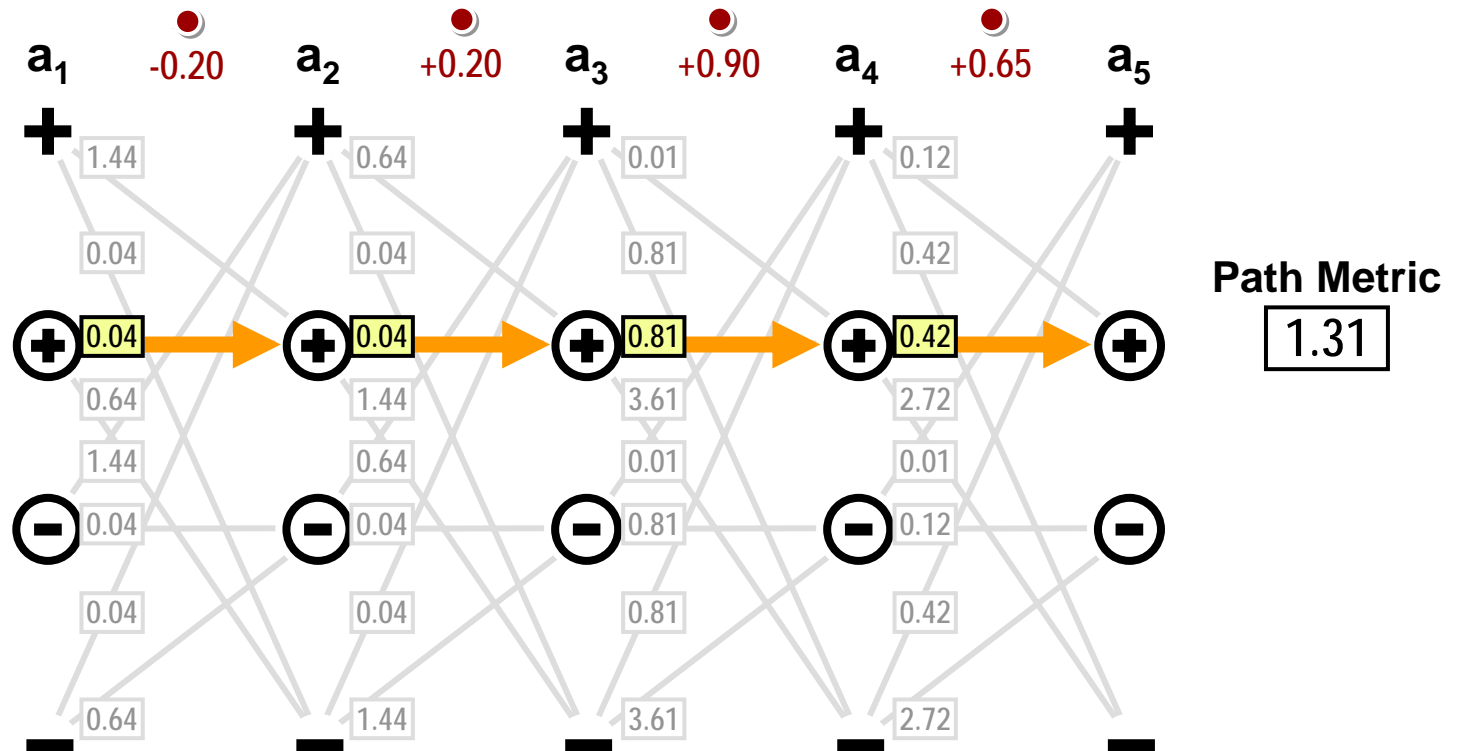
$$BM_1 = (\quad - m_1)^2$$

Computing Branch Metrics



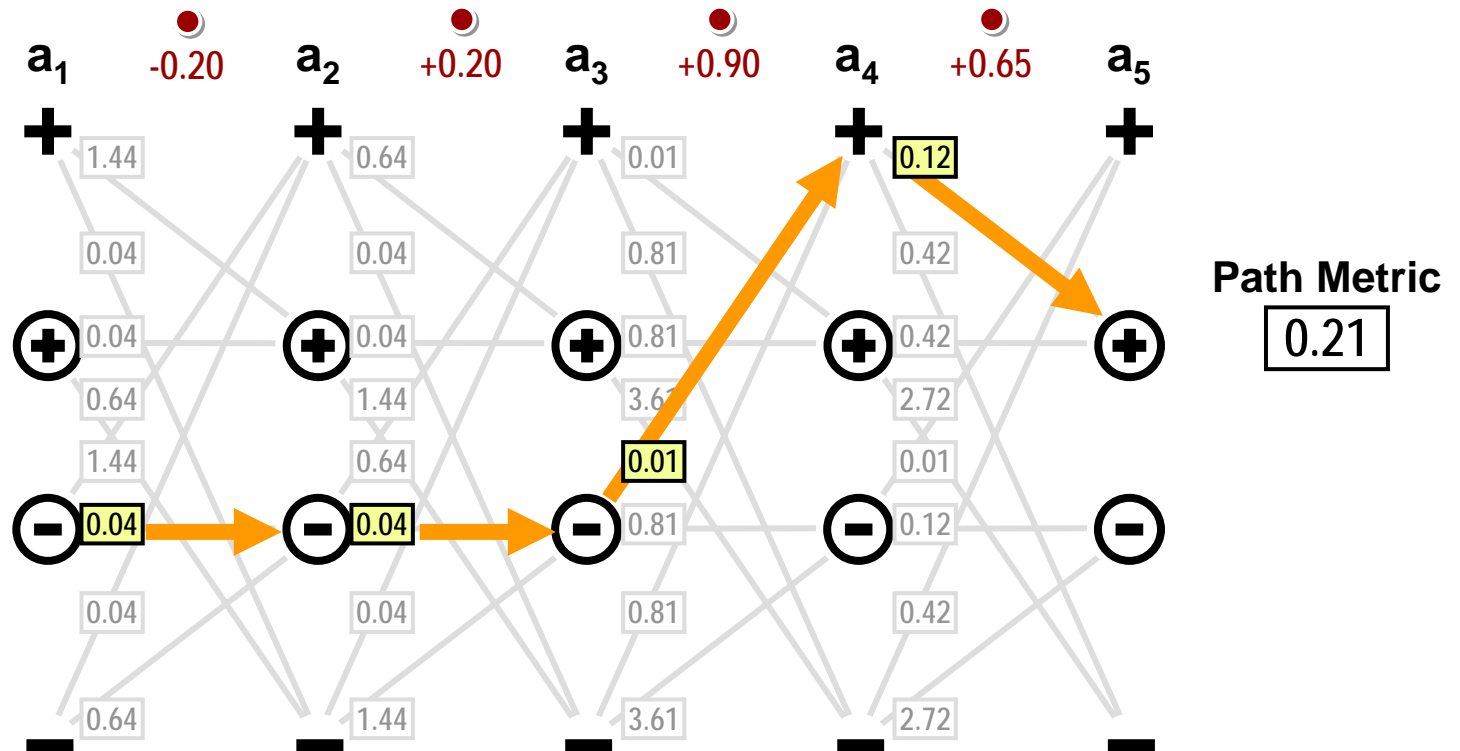
$$BM_i = (r_t - m_i)^2$$

Path Metrics



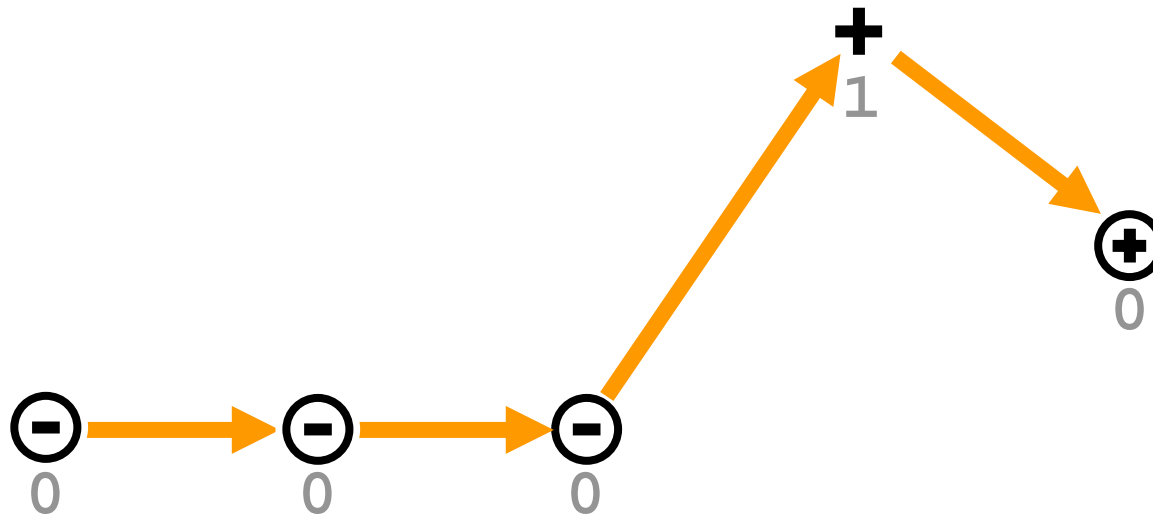
The path with the lowest cumulative total is the most likely sequence

Path Metrics



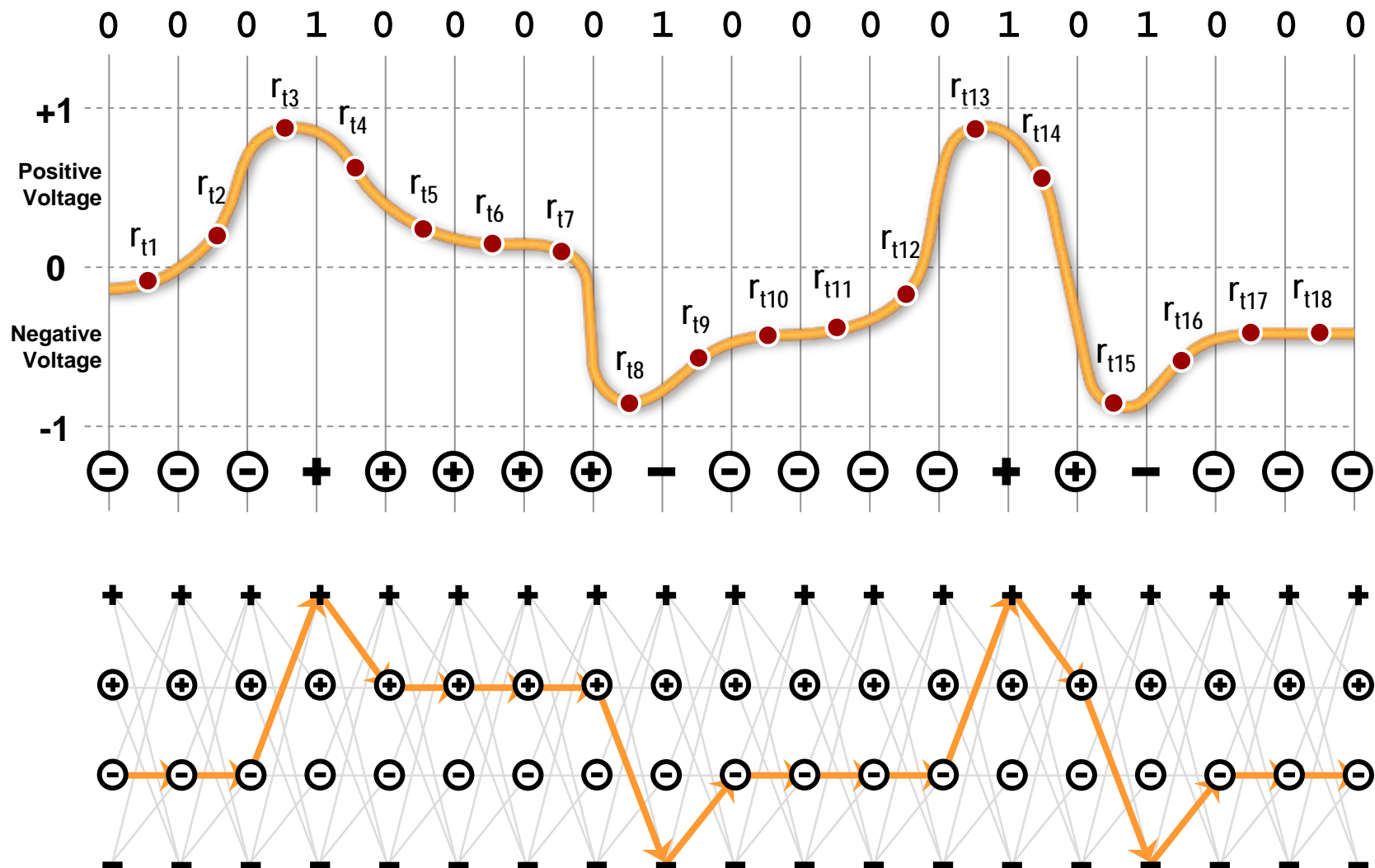
The path with the lowest cumulative total is the most likely sequence

Path Metrics



The path with the lowest cumulative total is the most likely sequence

Determining the Bit Sequence



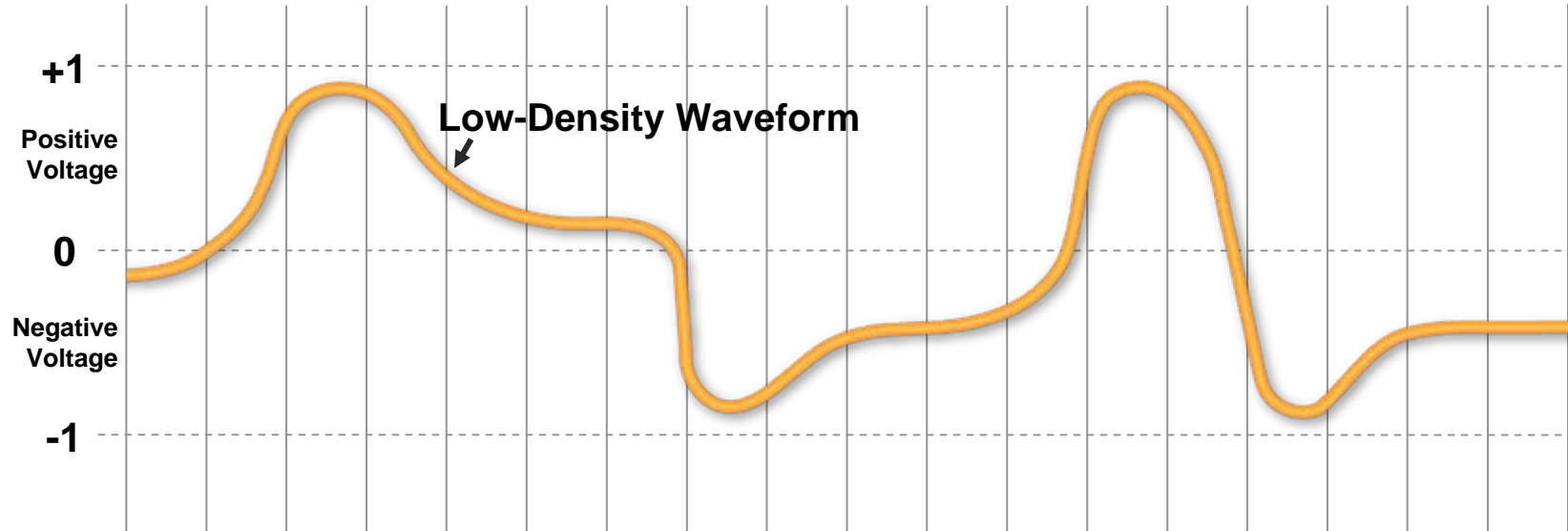
Determining the Bit Sequence

0 0 0 1 0 0 0 0 1 0 0 0 0 1 0 1 0 0 0



Viterbi Detectors in a High Data Density Environment

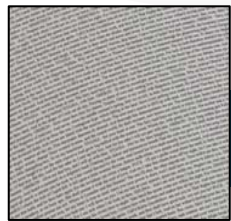
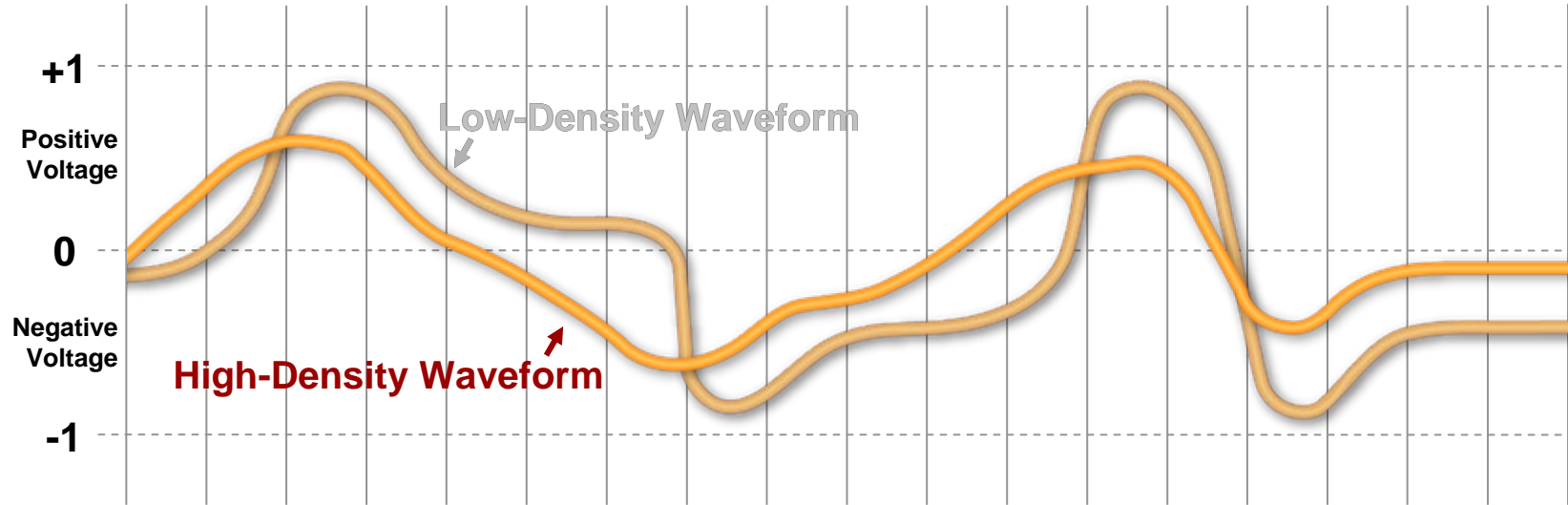
Viterbi Detectors in a High Data Density Environment



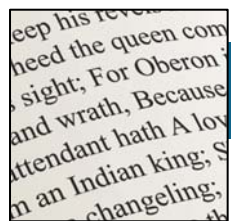
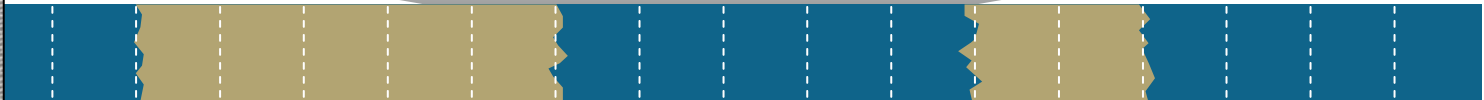
Low-Density Track



Viterbi Detectors in a High Data Density Environment



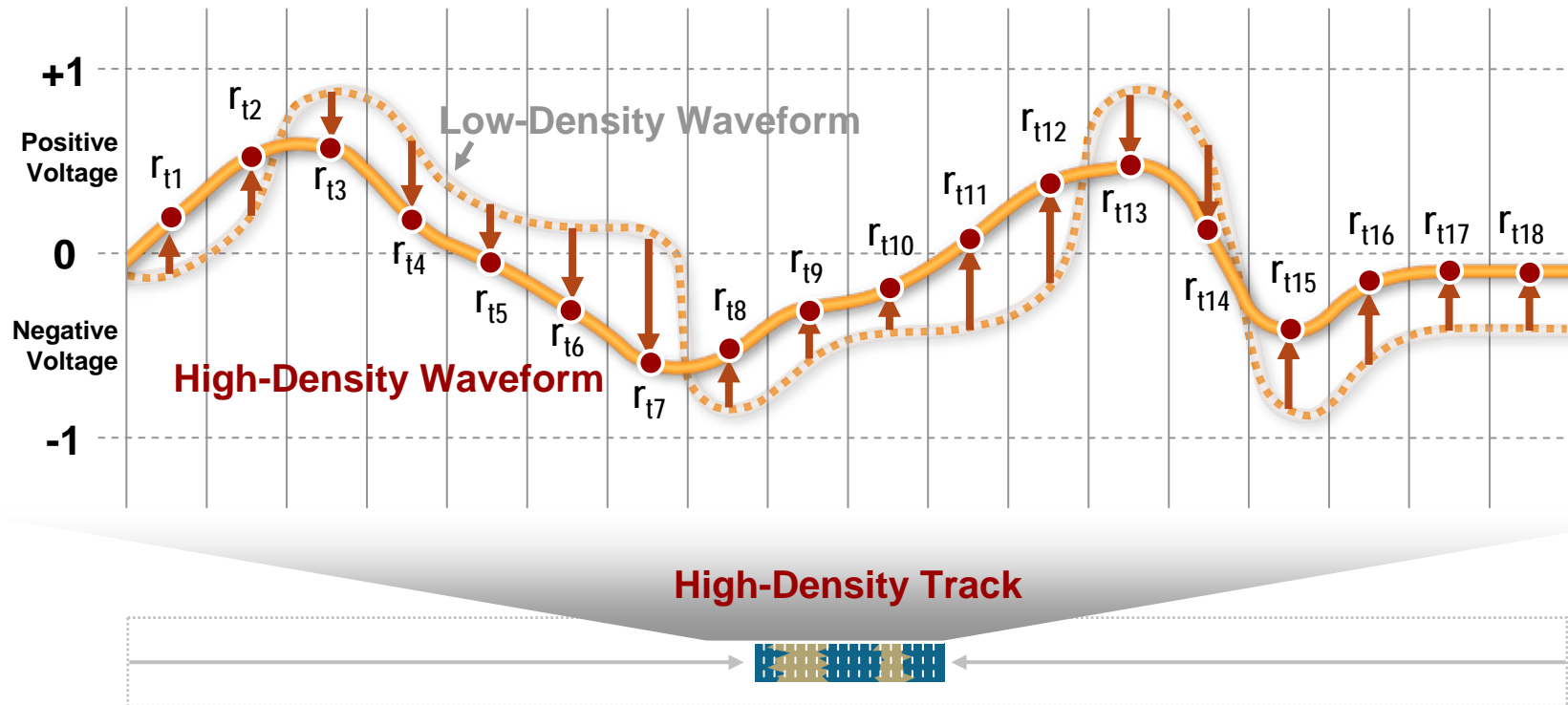
High-Density Track



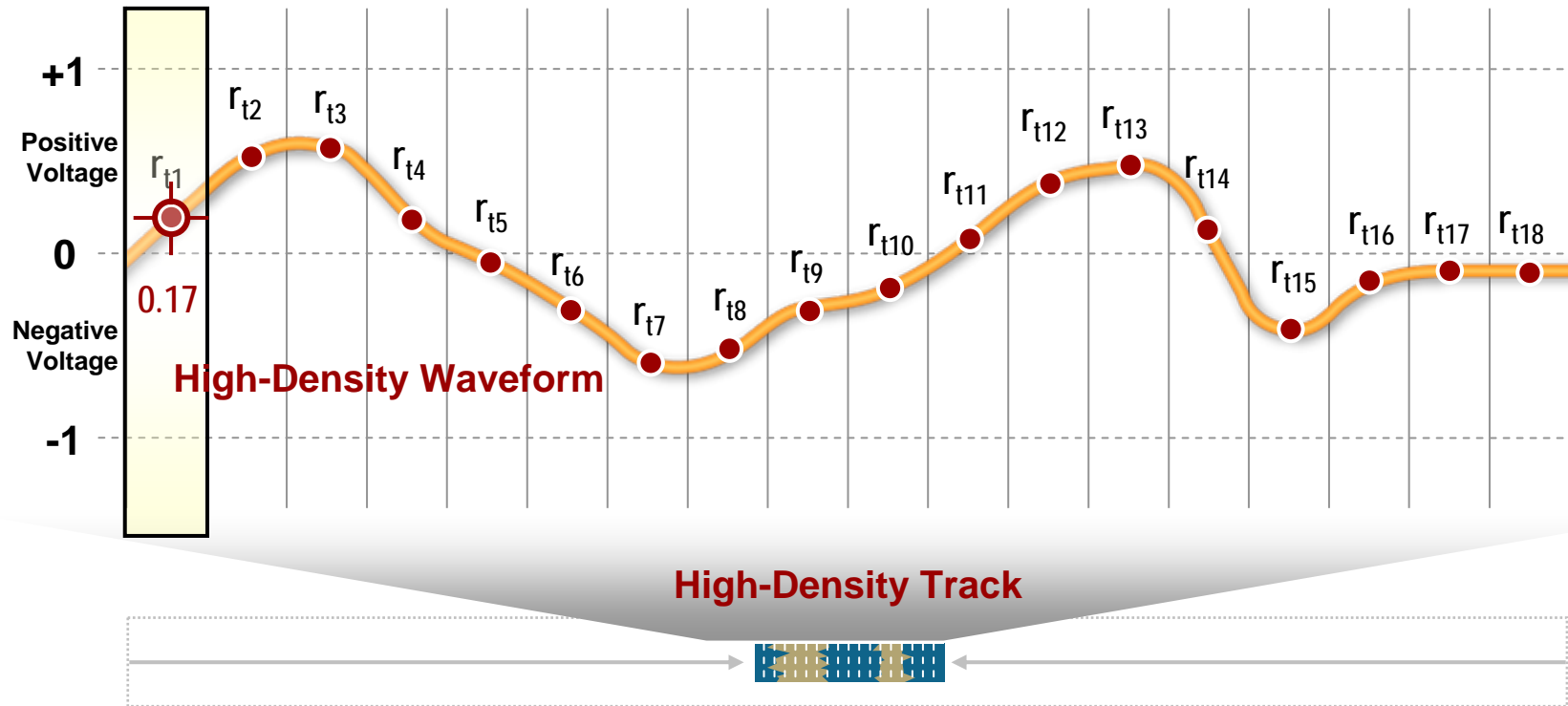
Low-Density Track



Viterbi Detectors in a High Data Density Environment



Viterbi Detectors in a High Data Density Environment



$$BM_1 = (\quad - m_1)^2$$

Viterbi Detectors in a High Data Density Environment

Low-Density Reading

r_{t1}
●
-0.20

$BM_1 = 1.44$

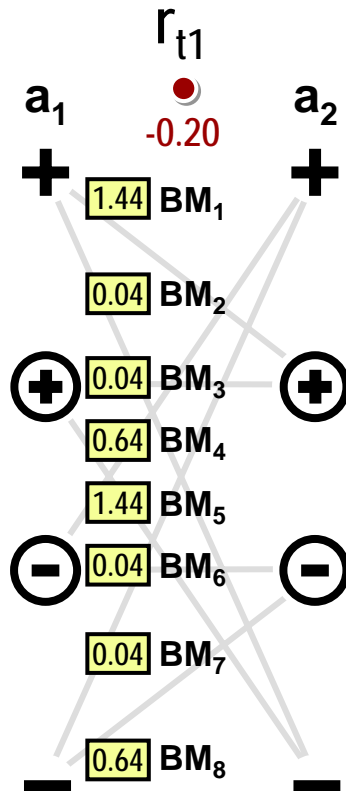
High-Density Reading

r_{t1}
●
+0.17

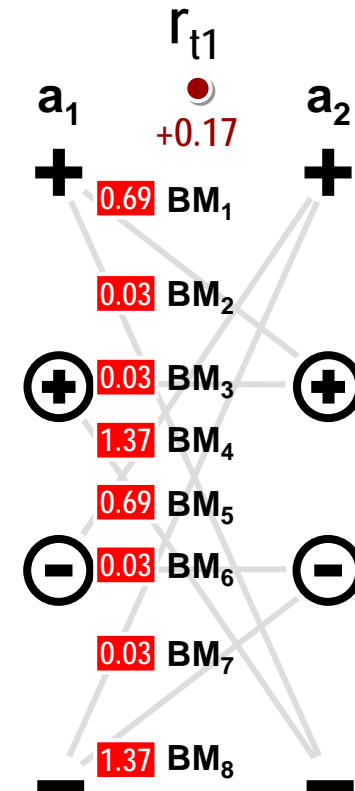
$BM_1 = 0.69$

Viterbi Detectors in a High Data Density Environment

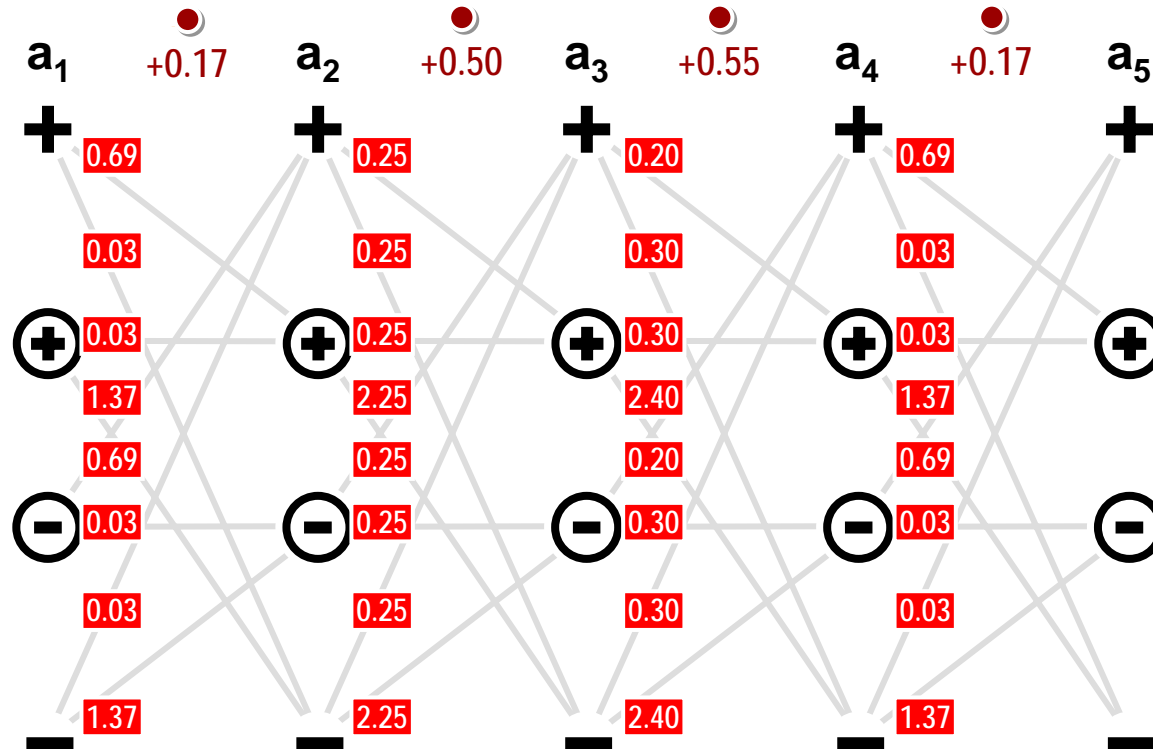
Low-Density Reading



High-Density Reading

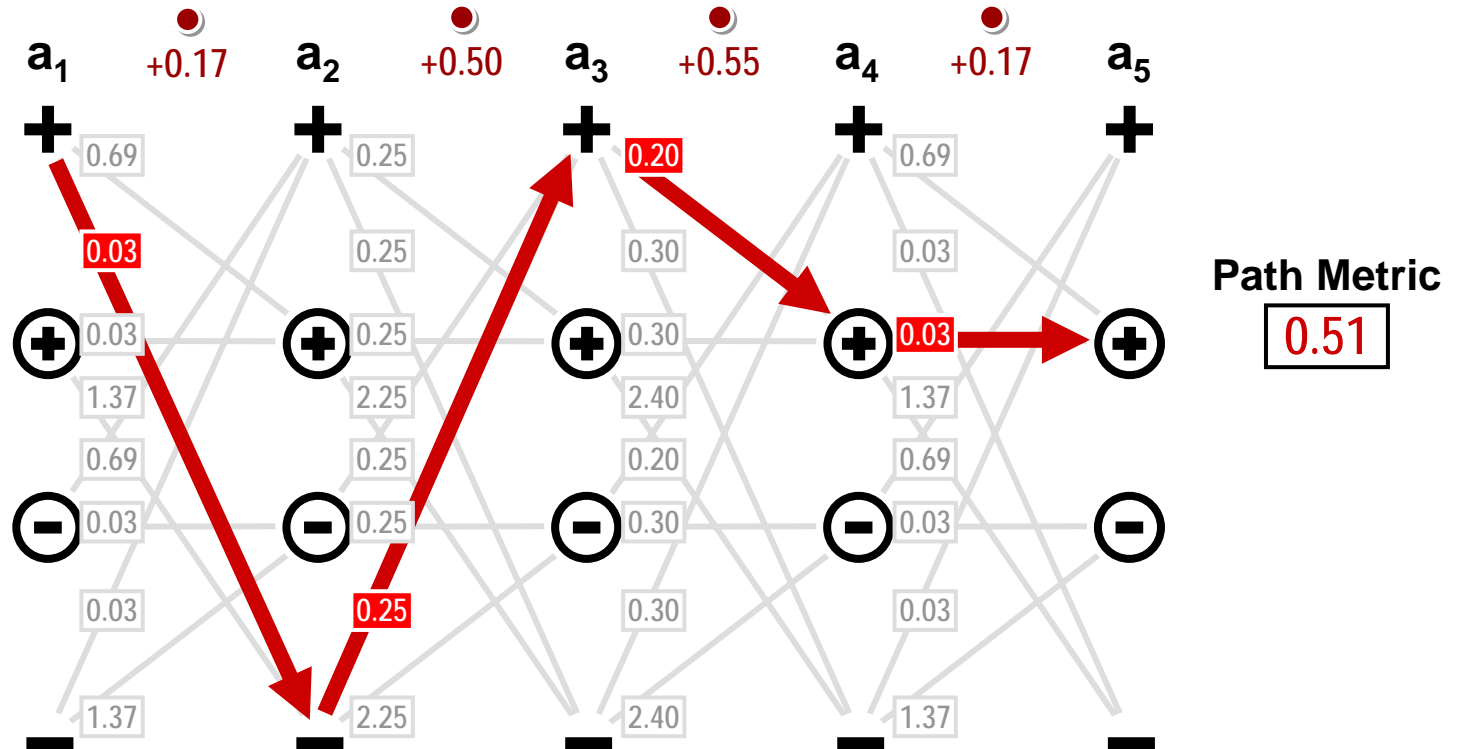


High Data Density Branch Metrics



$$BM_i = (r_t - m_i)^2$$

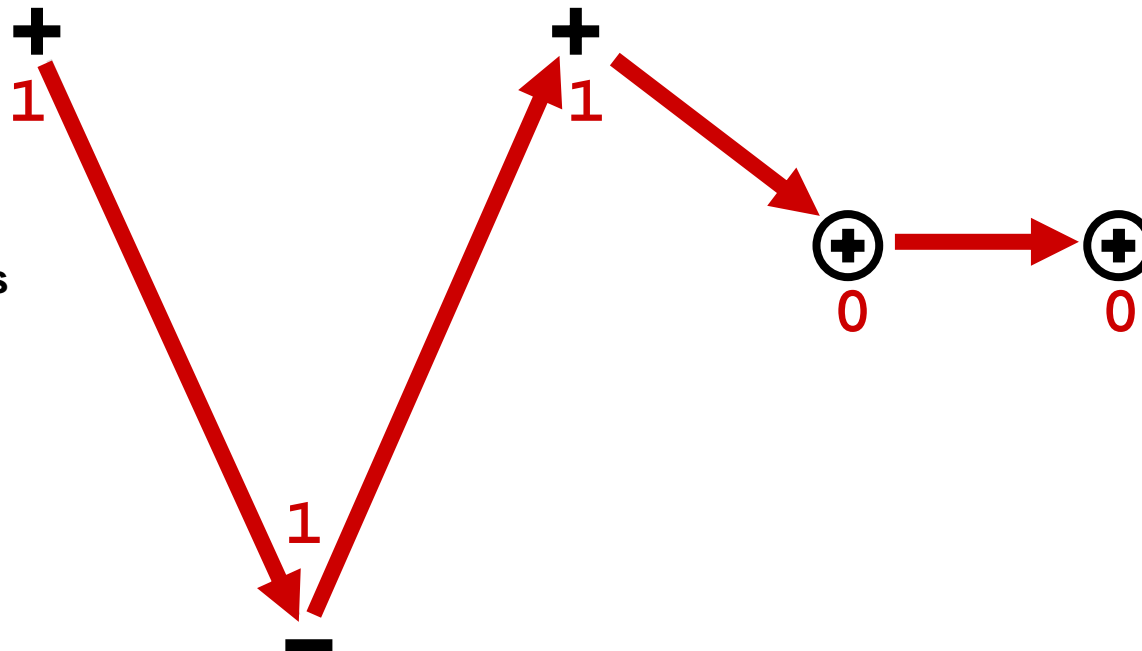
High Data Density Path Metric



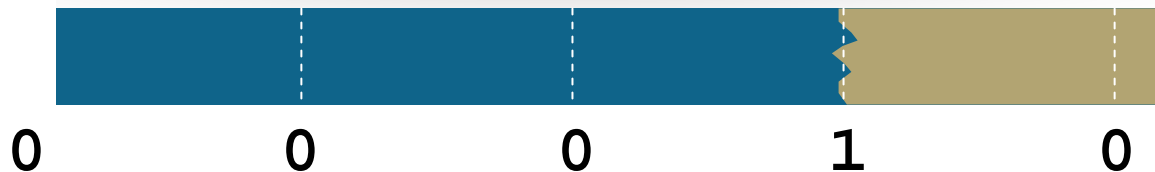
$$BM_i = (r_t - m_i)^2$$

High Data Density Path Metric

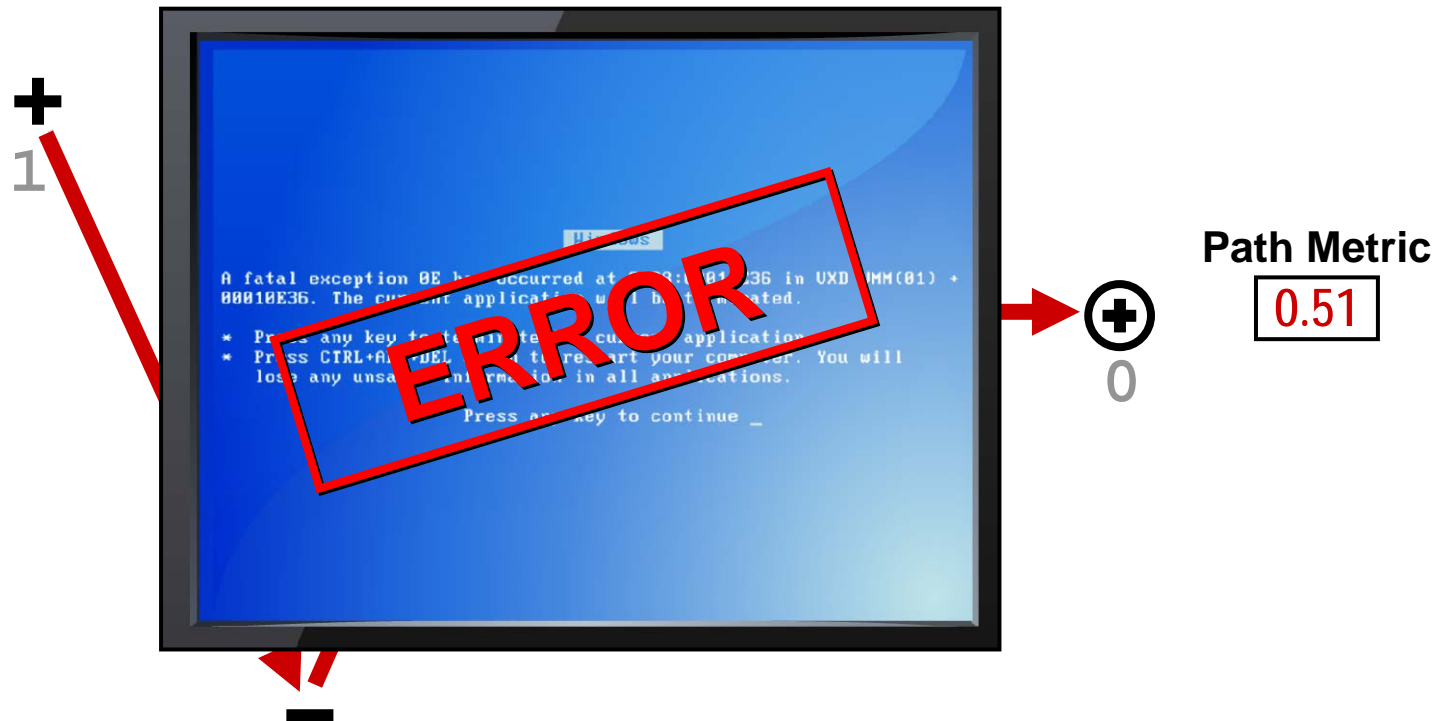
Bit sequence as
determined by
Prior Art Viterbi
detector:



Actual bit
sequence:



High Data Density Path Metric

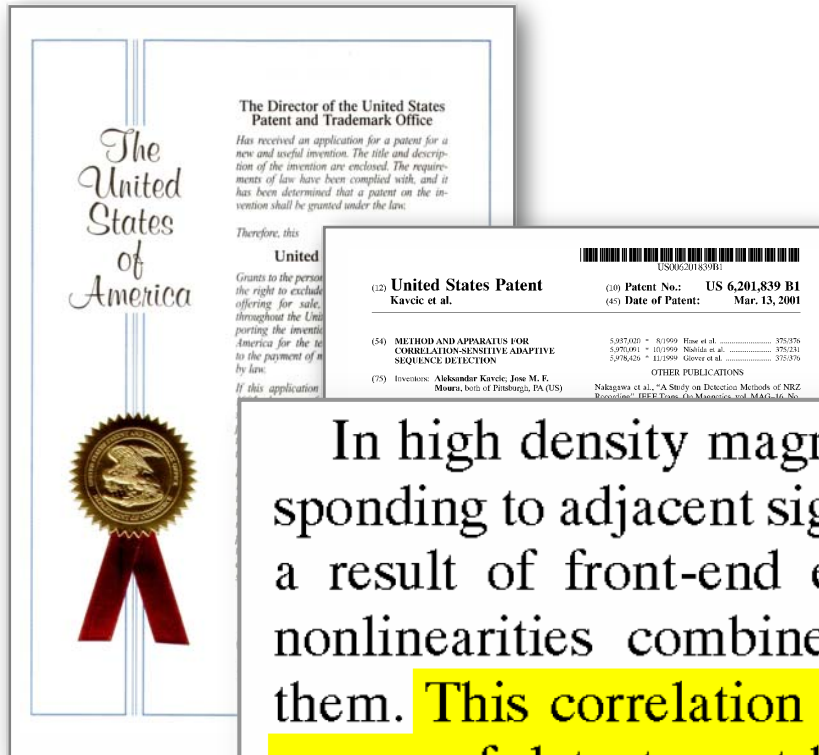


$$BM_i = (r_t - m_i)^2$$

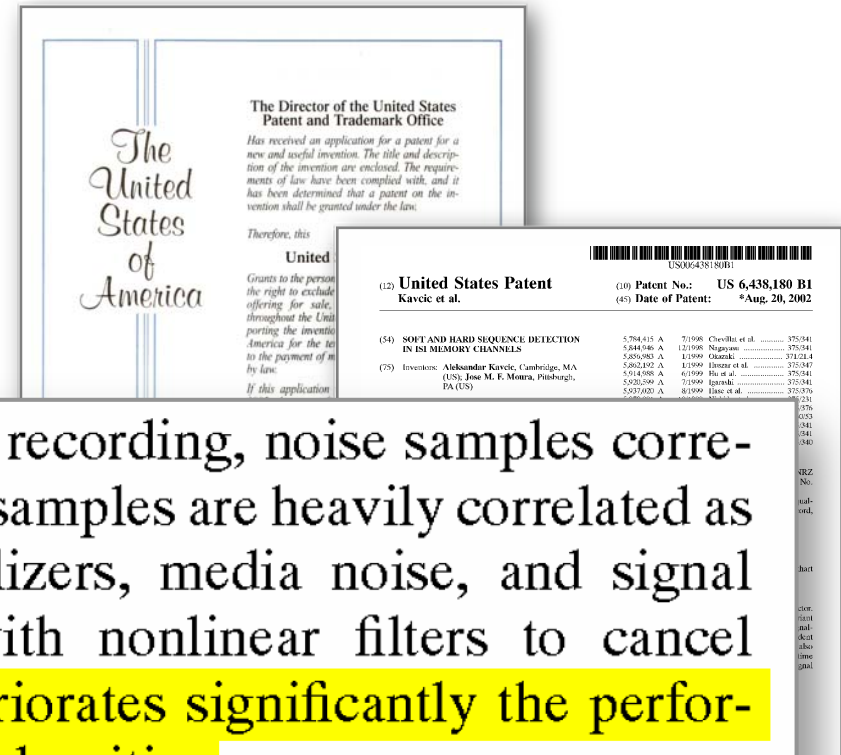
Kavcic-Moura Detector

The Kavcic-Moura Patents

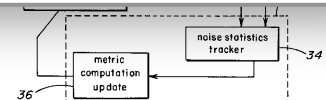
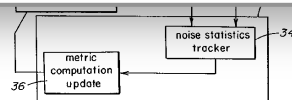
U.S. Patent 6,201,839



U.S. Patent 6,438,180

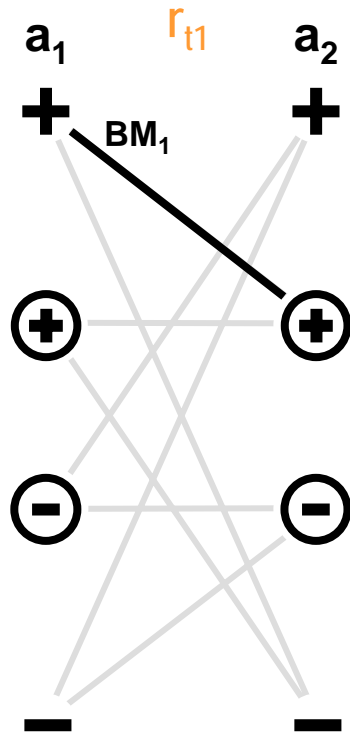


In high density magnetic recording, noise samples corresponding to adjacent signal samples are heavily correlated as a result of front-end equalizers, media noise, and signal nonlinearities combined with nonlinear filters to cancel them. This correlation deteriorates significantly the performance of detectors at high densities.





Prior Art Branch Metrics



Computing Branch Metric 1 (BM_1)

Prior Art

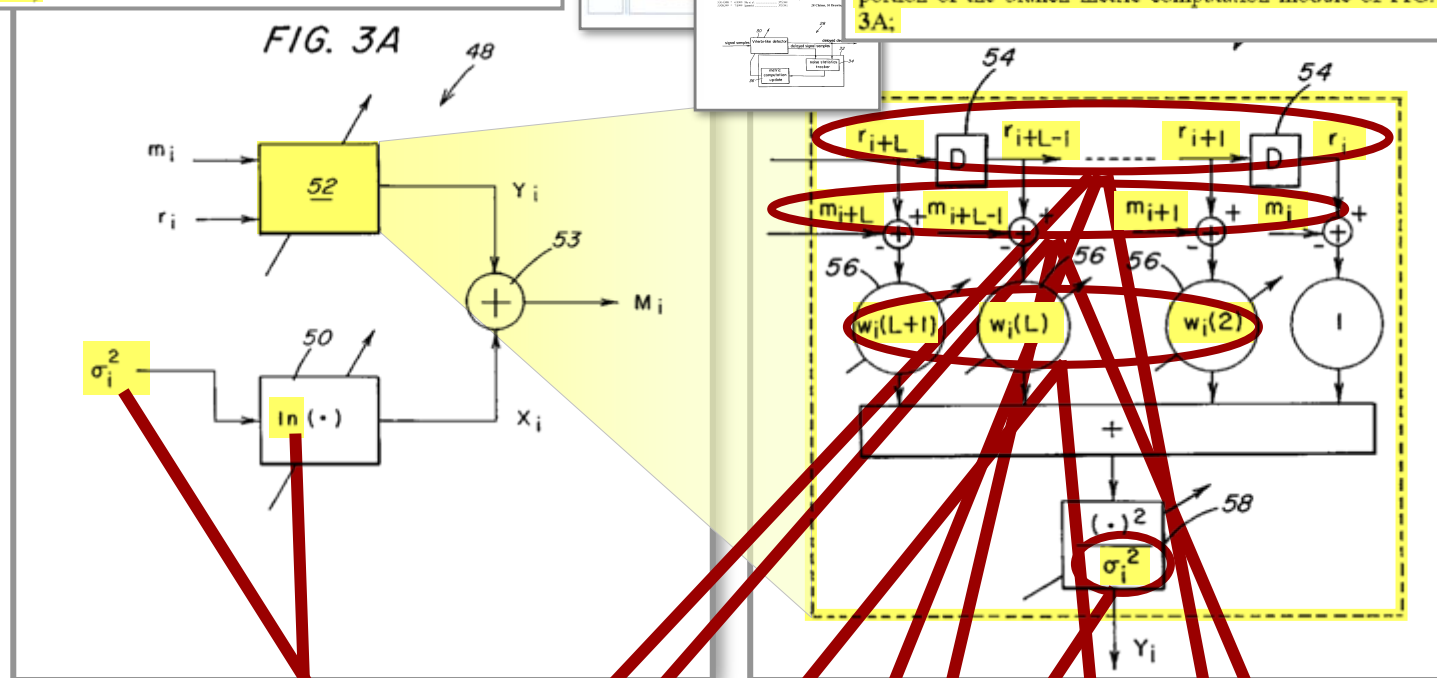
$$BM_1 = (r_{t1} - m_1)^2$$

Kavcic-Moura Branch Metrics

$$M_i = \log \det \frac{C_i}{\det C_i} + N_i^T C_i^{-1} N_i - N_i^T C_i^{-1} u_i \quad (13)$$

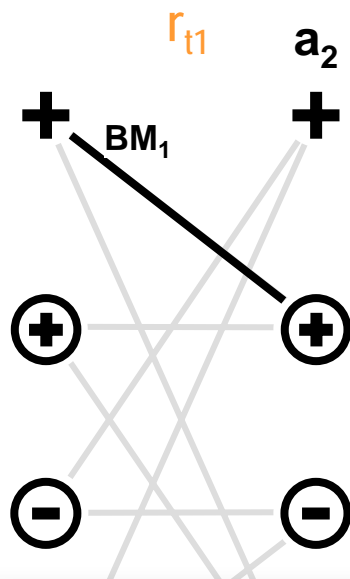
FIG. 3A illustrates a block diagram of a branch metric computation circuit 48 that computes the metric M_i for a branch of a trellis, as in Equation (13). Each branch of the

FIG. 3A is an illustration of a branch metric computation module;



$$BM_1 = \log \sigma_1^2 + \frac{[(r_{t1}-m_1) + w_{1(2)} \cdot (r_{t2}-m_{1(2)}) + w_{1(3)} \cdot (r_{t3}-m_{1(3)})]^2}{\sigma_1^2}$$

Kavcic-Moura Branch Metrics



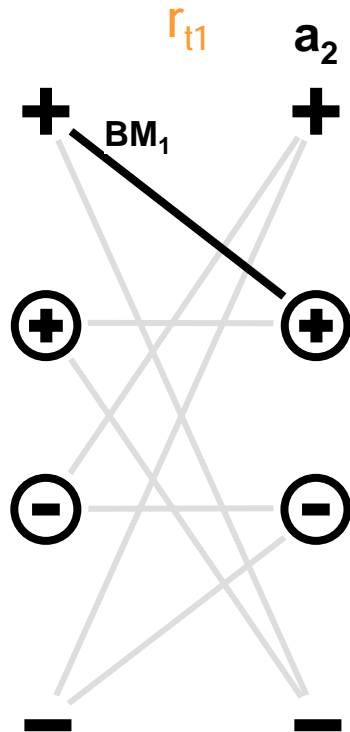
Computing Branch Metric 1 (BM_1)

Kavcic-Moura utilizes a novel equation to calculate a more accurate branch metric

Correlation-sensitive branch metric. In the most general case, the correlation length is $L > 0$. The leading and trailing ISI lengths are K_l and K_t , respectively. **The noise is now considered to be both correlated and signal-dependent.** Joint

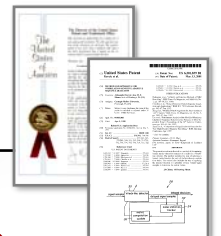
$$BM_1 = \log \sigma_1^2 + \frac{[(r_{t1} - m_1) + w_{1(2)} \cdot (r_{t2} - m_{1(2)}) + w_{1(3)} \cdot (r_{t3} - m_{1(3)})]^2}{\sigma_1^2}$$

Kavcic-Moura Branch Metrics

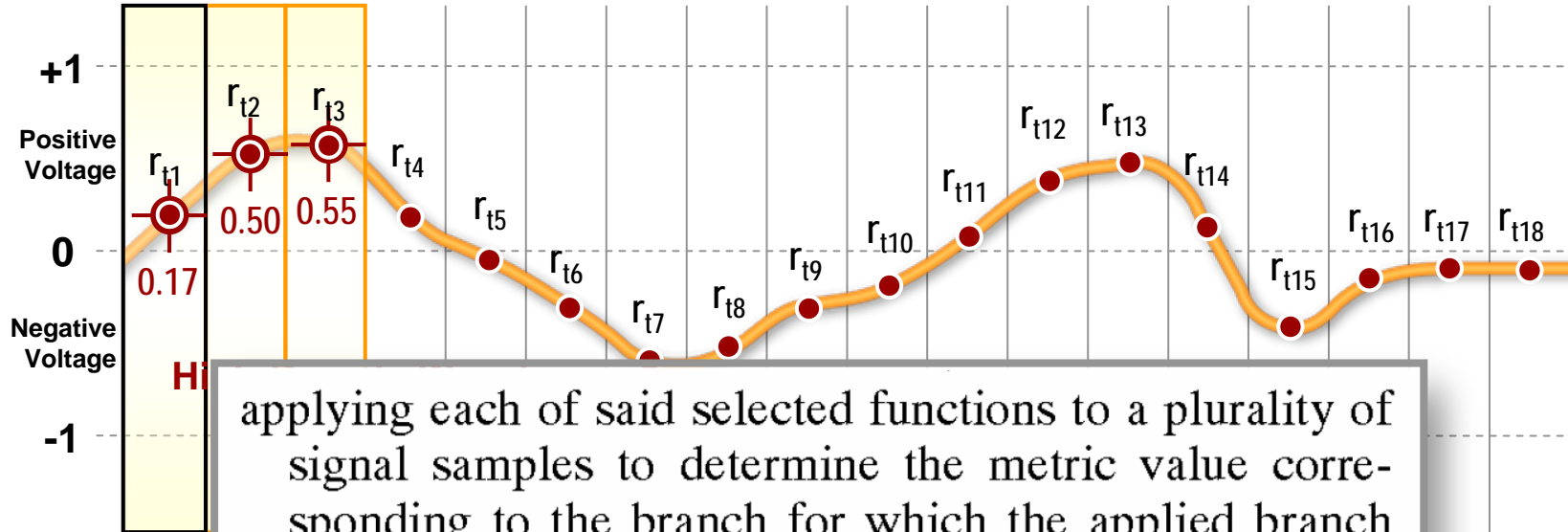


Computing Branch Metric 1 (BM_1)

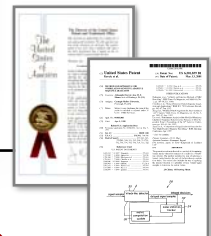
$$BM_1 = \log \sigma_1^2 + \frac{[(r_{t1} - m_1) + w_{1(2)} \cdot (r_{t2} - m_{1(2)}) + w_{1(3)} \cdot (r_{t3} - m_{1(3)})]^2}{\sigma_1^2}$$



Kavcic-Moura Branch Metrics

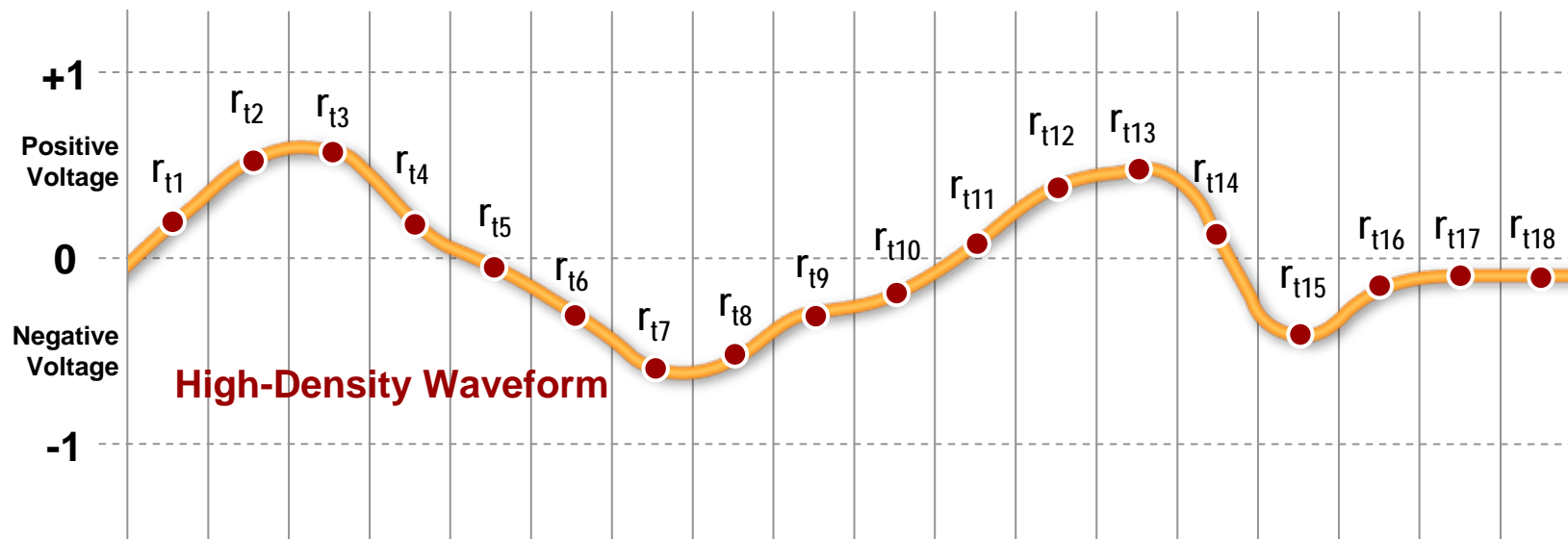


Source:
'839 Patent Claim 1 (13:61-14-2)

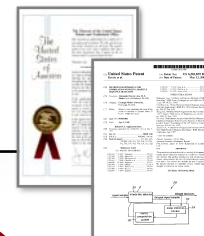


$$BM_1 = \log \sigma_1^2 + \frac{[(r_{t1} - m_1) + w_{1(2)} \cdot (r_{t2} - m_{1(2)}) + w_{1(3)} \cdot (r_{t3} - m_{1(3)})]^2}{\sigma_1^2}$$

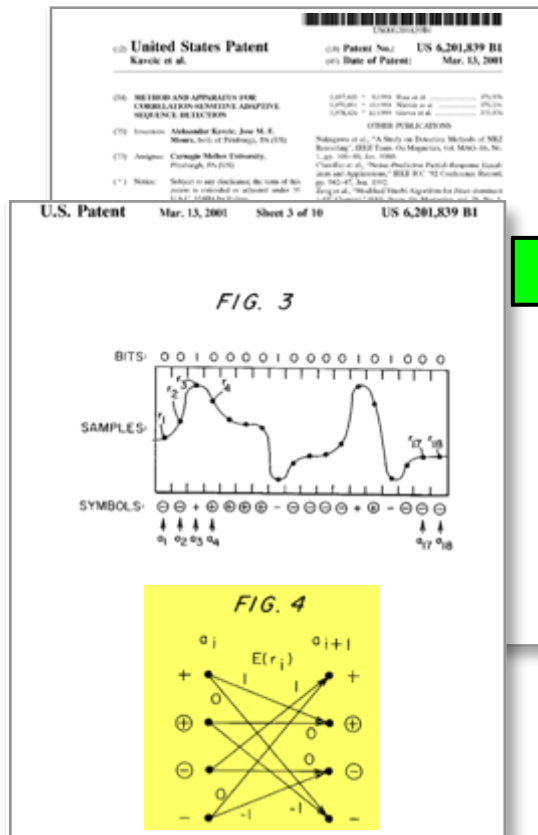
Kavcic-Moura Branch Metrics



$$BM_1 = \log \sigma_1^2 + \frac{[(r_{t1} - m_1) + w_{1(2)} \cdot (r_{t2} - m_{1(2)}) + w_{1(3)} \cdot (r_{t3} - m_{1(3)})]^2}{\sigma_1^2}$$



The Kavcic-Moura Patents



Target Values

